

INSTITUT NATIONAL DE RECHERCHE EN INFORMATIQUE ET EN AUTOMATIQUE

# Project-Team SIMPAF

# SImulation and Modelling for PArticles and Fluids

Lille - Nord Europe



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The SIMPAF project mainly emanates from the PDE team of the department Paul Painlevé (UMR 8524 of CNRS) of the University of Sciences and Technologies of Lille (USTL); it has also strong interaction with other math departments in the North area (Amiens, Valenciennes) and in Paris.

# 1. Team

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# 2. Overall Objectives

# 2.1. Overall Objectives

The project aims at:

- Studying models that describe the evolution of a fluid and/or of a large number of particles;
- Discussing the relevance and the range of validity of these models;
- Analyzing connections between different levels of modelling;
- Developing efficient numerical methods to compute the solutions of such models.

# 3. Scientific Foundations

# **3.1. PDEs for Particles and Fluids**

**Keywords:** Asymptotic analysis, Computational Fluid Dynamics, Conservation Laws, Fluid Mechanics, Hyperbolic Systems, Kinetic Equations, PDEs, Parabolic Systems, Plasma Physics.

The scientific activity of the project is concerned with PDEs arising from the physical description of particles and fluids. It covers various viewpoints:

- At first, the words "particles and fluids" could simply mean that we are interested independently in models for particles, which can either be considered as individuals (which leads to "*N*-particle models", *N* ranging from 1 to many) or through a statistical description (which leads to kinetic equations) as well as in models for fluids like Euler and Navier-Stokes equations or plasma physics.
- However, many particle systems can also be viewed as a fluid, via a passage from microscopic to macroscopic viewpoint, that is, a hydrodynamic limit.
- Conversely, a fruitful idea to build numerical solvers for hyperbolic conservation laws consists in coming back to a kinetic formulation. This approach has recently motivated the introduction of the so-called kinetic schemes.
- Eventually, one of the main topics of the project is to deal with models of particles interacting with a fluid.

By nature these problems describe multiscale phenomena and one of the major difficulties when studying them lies in the interactions between the various scales: number of particles, size, different time and length scales, coupling...

The originality of the project is to consider a wide spectrum of potential applications. In particular, the word "particles" covers various and very different physical situations, like for instance:

- charged particles: description of semi-conductor devices or plasmas;
- photons, as arising in radiative transfer theory and astrophysics;
- neutrons, as arising in nuclear engineering;
- bacteria, individuals or genes as in models motivated by biology or population dynamics;
- planets or stars as in astrophysics;
- vehicles in traffic flow modelling;

- droplets and bubbles, as in Fluid/Particles Interaction models which arise in the description of sprays and aerosols, smoke and dust, combustion phenomena (aeronautics or engine design), industrial process in metallurgy...

We aim at focusing on all the aspects of the problem:

- Modelling mathematically complex physics requires a deep discussion of the leading phenomena and the role of the physical parameters. With this respect, the asymptotic analysis is a crucial issue, the goal being to derive reduced models which can be solved with a reduced numerical cost but still provide accurate results in the physical situations that are considered.
- The mathematical analysis of the equations provides important qualitative properties of the solutions: well-posedness, stability, smoothness of the solutions, large time behavior... which in turn can motivate the design of numerical methods.
- Eventually, we aim at developing specific numerical methods and performing numerical simulations for these models, in order to validate the theoretical results and shed some light on the physics.

The team has been composed in order to study these various aspects simultaneously. In particular, we wish to keep a balance between modelling, analysis, development of original codes and simulations.

### **3.2.** Interactions of Micro- and Macroscopic Scales, Modelling and Simulations

**Keywords:** Asymptotic Preserving Schemes, Fluid-Particles Flows, Hydrodynamic Limit, Radiative Transfer, Statistical Physics.

#### 3.2.1. Reduced Models; Hydrodynamic Limits

In the study of kinetic equations, it is a very usual strategy to perform a hydrodynamic limit, and then to get rid of the velocity variable and replace the kinetic equation by a convection-diffusion model. This kind of derivation is well established, under various forms, and in several fields of applications: neutron transport, semiconductor theory, SHE<sup>1</sup> models... However, several questions of great interest have not yet been solved:

- The computation of the convection-diffusion coefficients of the limit equation, a question which leads to additional difficulties when the small mean free path asymptotics are combined with a homogeneization limit. This problem is motivated by applications in nuclear engineering. In this case, the effective coefficients are defined through auxiliary equations and suitable averages of the oscillatory coefficients.

- Some recent works have revealed the formation of singularities in the solutions of some limit convectiondiffusion equations, while the original kinetic equation has globally defined solutions. This is due to a coupling in the definition of the convective term with the macroscopic density. This singularity formation is typical of aggregation dynamics. It occurs in models with gravitational forces in astrophysics, and chemotaxis models in biology. Therefore, the natural problems are either to provide a sharp analysis (theoretical and/or based on numerics) of the singularity formation, or to complete the model to avoid such trouble.

- A crucial question for applications is to write models for intermediate regimes, for small but non zero values of the mean free path. Such models are required to remain solvable with a moderate computational cost, and to preserve more features from the kinetic level (as for instance finite speeds of propagation, which is lost with a diffusion equation). An example of such an intermediate model is the moment system obtained by using a closure by Entropy Minimization. We have proved recently that this model is indeed consistent with the diffusion approximation, and we propose an original scheme to treat these equations numerically. We introduce a relaxation strategy which in turn is naturally amenable to the use of asymptotic preserving splitting methods and anti-diffusive schemes for transport equations that are developed in the team. Therefore, we can compare various limited flux models and discuss on numerics their properties and advantages.

<sup>&</sup>lt;sup>1</sup>referring to the standard vocabulary in Physics for Spherical Harmonics Expansion

#### 3.2.2. Radiative Transfer Theory

We are interested in the equations of the radiative transfer theory which are motivated by the description of high temperature combustion processes (spacecraft propulsion, reentry problems), space observation, nuclear weapons engineering, or inertial confinement fusion. Such problems can be described by a coupling between kinetic and macroscopic equations that comes from the "collision term", through energy, or energyimpulsion, exchanges. The hydrodynamic limit yields coupled macroscopic equations, with possibly two distinct temperatures: the temperature of the radiations and the temperature of the material. Taking into account Doppler and relativistic effects adds convective terms, which in turn might give rise to the formation of specific singularities.

The interesting points can be summarized as follows:

- The derivation of the reduced models, based on modeling arguments, is an issue, bearing in mind to describe a complete hierarchy of models;

- The coupling induces non trivial effects on the structure of the hydrodynamics system, which can modify strongly the qualitative properties of the solutions. In particular, the radiative transfer equations might exhibit non standard shocks profiles, with possible discontinuities. The computation of such discontinuous shock profiles requires a very accurate and nondiffusive numerical scheme for the convective terms. This also leads to the delicate question of the stability of travelling waves solutions.

These topics are the object of a very intense research activity e.g. at the Department of Computational Physics of the Los Alamos National Laboratory as well as at the French Atomic Energy Agency (CEA). We develop alternative numerical methods, based on tricky splitting approaches. When dealing with kinetic models, such methods have to be specifically designed to preserve the asymptotic properties of the model. In this approach, one computes on a time step the evolution of the unknown due the convective terms, which will be handled by antidiffusive schemes (see the paragraph Conservation Laws below), and on the next time step, we treat source and interaction terms, that can be nonlocal and/or stiff. This leads to a fully explicit scheme which provides accurate results for a cheap numerical cost and which does not require a tedious inversion step as the implicit methods usually do. We are able to treat numerically the full coupling of radiation with hydrodynamics (Euler equations) in the non equilibrium diffusion regime.

#### 3.2.3. Fluid/Particles Interactions

These models arise in the modelling of disperse suspensions in fluids, say droplet or bubble motion. Their study is motivated by applications to combustion, rocket propulsor engineering, biology, aerosols engineering, or for certain industrial processes... The main effect to take into account is the Stokes drag force, which is proportional to the relative velocity between the particle and the surrounding fluid  $F(t, x, v) = \gamma(u(t, x) - v)$ . However, modelling remains a major issue in this field; in particular, here are some important questions :

- Complementary effects can be taken into account: the so-called Basset force, or the added mass effect, etc... For instance, when particles flow in a pipe, a phenomenological lift force, proportional to  $v \times (v - u)$ , has been proposed to mimic the tendency of particles to concentrate at the center of the pipe. Even though moderate in strength, such a force can have crucial effects on blood flows, or on industrial processes of steel production.

- Up to now, there are only a few contributions on the description of size variations, by coagulation or fragmentation and break-up. However, in practical situations, as for combustion or biology applications, these phenomena cannot be neglected.

- Of course, the coupling with the evolution of the surrounding fluid is a crucial question that leads naturally to problems of asymptotics. Effects of "turbulence", which roughly means high and fast variations of u on the behavior of the particles, have been analyzed in some simplified situations.

The coupling with the Navier-Stokes or the Euler equations is a privileged subject for SIMPAF. Some asymptotics lead to two-phase flows models, that we are interested in investigating both from a theoretical and numerical point of view. In particular, the effect of an external force (gravitational or centrifugal) can lead to sedimentation profiles that are suspected to be stable; we would like to confirm these heuristics by a thorough numerical and theoretical study. Of course, such investigations require efficient numerical schemes to solve the fluid equations with source terms, which will be detailed in the next sections. To this end, we adapt to this framework the numerical schemes we develop for radiative transfer problems, based on splitting methods and a suitable use of the asymptotic expansion.

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### **3.3. Charged Particles**

**Keywords:** Euler-Maxwell equations, Euler-Poisson equations, Magnetized plasmas, Ohm's law, Plasma Physics, Spacecraft charge modeling, Vlasov-Maxwell equations, Vlasov-Poisson equations.

#### 3.3.1. Modeling of Plasma Confinement

Plasmas, the fourth state of the matter, play an important role in many branches of physics, such as thermonuclear fusion research, astrophysics and space physics. A plasma is a (partially) ionized gas where charged particles interact via electromagnetic fields. Since the announcement of the creation of the experimental fusion reactor ITER, and with the progress on the ICF<sup>2</sup> program, plasmas and their modelling got a renewed interest.

The nuclear fusion mechanisms result from the strong confinement of charged particles, either by inertial confinement (nuclear fusion reactions are initiated by heating and compressing a target - a pellet that most often contains deuterium and tritium - by the use of intense laser or ion beams) or by the - more promising - magnetic fusion confinement. The tokamaks are experimental devices which produce a toroidal magnetic field for confining a plasma.

The description of these phenomena is extremely complex and leads to delicate problems in mathematical analysis and numerical simulation. Actually, plasmas may be described with various levels of detail. The simplest possibility is to treat the plasma as a single fluid governed by the Navier Stokes Equations. A more general description is the two-fluid picture, where the ions and electrons are considered to be distinct. If electric or magnetic fields are present, then the Maxwell equations will be needed to describe them. The coupling of the description of a conductive fluid to electromagnetic fields is known generally as magnetohydrodynamics, or simply MHD.

For some cases the fluid description is not sufficient. Then, the kinetic models may become useful. Kinetic models include information on distortions of the velocity distribution functions with respect to a Maxwell-Boltzmann distribution. This may be important when currents flow, when waves are involved, or when gradients are very steep.

The main mathematical difficulties are therefore linked to the conjunction of the following elements

- these two types of models are strongly nonlinear,
- the unknowns depend on the time and space variables and, in the case of kinetic models, also on the velocity variables. Therefore, we can be led to work with variables of 1 + 3 + 3 dimensions,
- there exist many very different scales (time scale, characteristic length ...)

The numerical resolution of a complete system of equations, with meshes adapted to the lower scales, leads to prohibitive computational costs both in terms of memory and time. The derivation of new reduced models, corresponding to relevant asymptotic regimes (high magnetic field for example), is therefore a crucial issue. Moreover, very serious efforts must be done on the numerical methods that are used in order to reproduce the typical phenomena. This work depends on the one hand on seriously thinking over the models, the physical parameters, their typical respective scales, and on the other hand over some arguments of asymptotic analysis, which can particularly call on deterministic or random homogeneization.

<sup>&</sup>lt;sup>2</sup>Inertial Confinement Fusion

#### 3.3.2. Spacecraft Environment

Satellites in geostationary and low Earth orbits naturally evolve in a plasma. This ionized environment induces some perturbations which may lead to many kind of faults and to the partial or complete loss of a mission. The satellites are covered by dielectric coatings in order to protect them against thermal radiations. Electrons and ions species of the space plasma interact with the external surfaces of the satellite and modify their electrostatic charges. This effect produces potential differences between the satellite surfaces and its electric mass. When the electric field exceeds a certain level, an electrostatic discharge appears. This electric current pulse is able to disrupt the equipments, to damage the external surfaces and even to destroy some electronic components. The plasma may also be created by an other source : the electric thrusters. This new propulsion device uses the electric energy supplied by solar arrays to speed up charged species. It is more and more used in satellite industry and has preference over the classical chemical propulsion. Indeed, the latter needs a very large amount of propellant inducing an expensive rocket launch. On the one hand, the electric thrusters allow to significantly reduce the satellite weight. On the other hand, it is necessary to understand their potential impacts on the other systems of the satellite.

This line of research, which continues former works of the team CAIMAN at Sophia Antipolis, is the object of a strong collaboration with the Department Research and Technology of the company Thales Alenia Space. In this context, the PhD of S. Borghol aims at deriving models specifically adapted to the LEO or PEO altitudes<sup>3</sup> instead of the standard GEO<sup>4</sup> framework. Analysis of the models and design of numerical schemes is also discussed. N. Vauchelet proposed several evolutions for the SPARCS code, including parallel procedures. A comparizon of different numerical schemes (Finite Volume, Semi-Lagrangian, Back Trajectory) to treat the Vlasov equations of spacecraft charging has been discussed in details.

#### 3.3.3. Effective Energy Dissipation Models for Charged Particles

In models of charge transport, say transport of electrons, a phenomenological friction force is generally introduced, which is proportional to the velocity v. Our idea is to go back to a more microscopic framework, with a description of the energy exchanges between the electrons and the surrounding medium. In turn, the dissipation of energy by the medium will lead to an effective friction force. The first contributions only model the transport of a unique particle, and we aim at considering now a plasma, through a statistical description. This yields a Vlasov-Poisson-like model. (More precisely, the kinetic equation is coupled to a finite, or infinite, set of oscillators.) This program requires efforts in modelling and analysis, but the questions are also really challenging for numerics, due, on the one hand, to the large number of degrees of freedom involved in the equation, and on the other hand, to the presence of stiff terms. In this way, we expect to be able to shed light on the range of validity of the Ohm law. Similar considerations also apply for heat transport and the derivation of the Fourier law.

### **3.4. Simulations of Complex Fluid Flows**

**Keywords:** Anti-Diffusive Schemes, Conservation Laws, Control, Finite elements methods, Finite volume methods, Turbulence, Viscous Flows.

#### 3.4.1. Conservation Laws

A major issue in the numerical analysis of systems of conservation laws is the preservation of singularities (shocks, contact discontinuities...). Indeed, the derivatives of the solutions usually blow-up in finite time. The numerical scheme should be able to reproduce this phenomenon with accuracy, i.e. with a minimum number of points, by capturing the profile of the singularity (discontinuity), and by propagating it with the correct velocity. The scheme should also be able to give some insight on the interactions between the possible singularities. Quite recently, new anti-diffusive strategies have been introduced, and successfully used on fluid mechanics problems. We focus on multidimensional situations, as well as on boundary value problems. Since a complete theory is not yet available, the numerical analysis of some prototype systems of conservation laws

<sup>&</sup>lt;sup>3</sup>Low Earth Orbit and Polar Earth Orbit respectively

<sup>&</sup>lt;sup>4</sup>Geostationary orbit

is a good starting point to understand multi-dimensional problems. In particular, a good understanding of the linear case is necessary. This is not achieved yet on the numerical point of view on general meshes. This question is particularly relevant in industrial codes, where one has to solve coupled systems of PDEs involving a complex coupling of different numerical methods, which implies we will have to deal with unstructured meshes. Thus, deriving non-dissipative numerical schemes for transport equations on general meshes is an important issue. Furthermore, transport phenomena are the major reason why a numerical diffusion appears in the simulation of nonlinear hyperbolic conservation laws and contact discontinuities are more subject to this than shocks because of the compressivity of shock waves (this is another reason why we focus at first on linear models).

The next step is to combine non-dissipation with nonlinear stability. An example of such a combination of preservation of sharp shocks and entropy inequalities has been recently proposed for scalar equations and is still at study. It has also been partially done in dimension one for Euler equations.

Of course, there are plenty of applications for the development of such explicit methods for conservation laws. We are particularly interested in simulation of macroscopic models of radiative hydrodynamics, as mentioned above. Another field of application is concerned with polyphasic flows and it is worth specifying that certain numerical methods designed by F. Lagoutière are already used in codes at the CEA for that purpose. We also wish to apply these methods for coagulation-fragmentation problems and for PDEs modelling the growth of tumoral cells; concerning these applications, the capture of the large time state is a particularly important question.

#### 3.4.2. Control in Fluid Mechanics

Nowadays, passive control techniques are widely used to improve the performances of planes or vehicles. In particular these devices can sensibly reduce energy consumption or noise disturbances. However, new improvements can be obtained through an active control of the flow, which means by activating mechanical devices. This is a very promising theme.

The first results are concerned with the control of the 2D compressible Navier-Stokes equations over a dihedral plane. The technical device consists in a small hole which allows to suck or to inject some fluid in the flow, depending on the pressure measured at another point. This improves the aerodynamics performance of the dihedral. Variants are possible, for instance by considering several such devices and taking into account the local properties of the flow.

Another work is concerned with simulation of the control of low Reynolds number flows (laminar regimes) over a backward facing step by imposing pulsed inlet velocities. Such a flow can be considered as a toy-model for the modelling of combustion phenomena. The goal is to understand and control vortex formations, by making the frequency and amplitude of the incoming fluid vary.

Recently, previous results on the step were generalized to the transitional regime, with a work of E. Creusé, A. Giovannini (IMFT Toulouse) and I. Mortazavi (EPI INRIA MC2, Bordeaux). The nonstationarity property of the uncontrolled flow allows to use some closed-loop control strategies. The control process is either a global one, by imposing a pulsed inlet velocity like for the laminar case, or a local one by the use of two horizontal jets located on the vertical side of the step.

Our current objective is now to apply such techniques on the "Ahmed body geometry", which can be considered as a first approximation of a vehicle profile. This work is performed in collaboration between E. Creusé and C.H. Bruneau (EPI INRIA MC2, Bordeaux) in the context of the research and innovation program on terrestrial transports supported by the ANR and the ADEME, leaded by Renault and PSA and managed by Jean-Luc Aider (ESPCI Paris). We have in mind to combine active and passive control strategies in order to reach efficient results, especially concerning the drag coefficient, on two and three dimensional simulations. Another important point consists in deriving more sophisticated control laws, using either adaptive or optimal control processes.

#### 3.4.3. Numerical Methods for Viscous Flows

In the large scale computations of fluid flows, several different numerical quantities appear that are associated to different eddies, structures or scales (in space as well as in time). An important challenge in the modelling of turbulence and of the energy transfer for dissipative equations (such as Navier-Stokes equations, reactiondiffusion equations) is to describe or to model, for the long time behavior, the interaction between large and small scales. They are associated to slow and fast wavelengths respectively. The multiscale method consists in modelling this interaction on numerical grounds for dissipative evolution equations. In Finite Elements and Finite Differences discretizations the scales do not appear naturally as in spectral approximations, their construction is obtained by using a recursive change of variables operating on nested grids; the nodal unknowns (Y) of the coarse grids are unchanged (they are of the order of magnitude of the physical solution) and those of the fine grids are replaced by proper error interpolation, namely the incremental unknowns (Z); the magnitude of the Zs is then "small". This allows to make a separation of the eddies in space (presence of nodal and incremental quantities) but also in frequency since the incremental unknowns are supported by the fine grids which capture the high frequencies while the nodal unknowns are defined on coarse grids which can represent only slow modes. Note that this approach differs from the LES model that proposes to split the flow into a mean value and a fluctuation component, the latter having small moments but not necessarily a small magnitude. This change of variable defines also a hierarchical preconditioner. It is well known that the (semi)explicit time marching schemes have their stability region limited by the high modes, so a way to enhance the stability is to tread numerically the scales (Y and Z) in a different manner. The inconsistency carried by the new scheme acts only on small quantities allowing for efficient and accurate schemes for the long time integration of the equations. We develop and apply this approach to the numerical simulation of Navier-Stokes equations in highly non stationary regimes. In this framework of numerical methods, we focus on the domain decomposition method together with multiscale method for solving incompressible bidimensional NSE; the stabilized explicit time marching schemes are also studied.

The already written code can be used to treat certain low Mach number models arising in combustion theory, as well as models describing mixing of compressible fluids arising for instance when describing the transport of pollutants. The interesting thing is that this kind of model can be derived by a completely different approach through a kinetic model. Besides, this model presents interesting features, since it is not clear at all whether solutions can be globally defined without smallness assumptions on the data. Then, a numerical investigation is very useful to check what the actual behavior of the system is. Accordingly, our program is two-fold. On the one hand, we will develop a density dependent Navier-Stokes code, in 2D, the incompressibility condition being replaced by a non standard condition on the velocity field. The numerical strategy we use mixes a Finite Element method for computing the velocity field to a Finite Volume approach to evaluate the density. As a by-product, the code should be able to compute a solution of the 2D incompressible Navier-Stokes system, with variable density. On the other hand, we wish to extend our kinetic asymptotic-based schemes to such problems.

# 4. Software

### 4.1. Simula+

**Keywords:** A posteriori Estimators, Finite Elements Methods, Linear Systems, Mesh Generation. **Participant:** Emmanuel Creusé [correspondant].

See the web page http://www.univ-valenciennes.fr/lamav/Simula+

The project Simula+ involves the LAMAV laboratory of the Valenciennes and Hainaut-Cambrésis University (UVHC) and LPMM laboratory from University and engineering schools ENSAM and ENIM of Metz. The project Simula+ aims at constructing C++ libraries devoted to scientific computing.

The motivation of this project is to organize the sharing and development of numerical routines. The final goal is to reduce significantly the time that is necessary to write scientific codes, and instead use more time to develop original methods and simulate applied problems. More precisely, the library contains three kinds of routines :

- <u>The MOL++ library</u>. This library is composed of some basic procedures of numerical linear algebra (direct and iterative methods for large space linear systems). These routines are developed both by the LAMAV and the LPMM. The goal is not to develop a wide range of solvers (a lot of commercial and free codes already exist to do it), but to have the only needed "material" for the following applications we are interested in.
- <u>The FEMOL++ library</u>. This library is composed of some procedures related to mesh refinement, finite element calculations, and *a posteriori* error estimators. It is developed by the LAMAV. Once again, the goal is not to do the same as well-known commercial codes, but to develop a specific work. The partial differential equations to be solved come mainly from fluid mechanics problems. They are rather standard (Laplacian, Stokes, *p*-Laplacian), and the geometries of the domains are academic. The originality of this work relies on the *a posteriori* error estimators derivation, for conform as well as for non conform finite element methods, and for isotropic as well as for anisotropic meshes. This topic is a large part of the research made by E. Creusé and S. Nicaise. These estimators are proved to be efficient and reliable from the theoretical point of view. The FEMOL++ library allows to illustrate and to validate these theoretical results by numerical computations.
- <u>The MateriOL++ library</u>. This library is composed of some procedures relative to the modelling of the multi-physics behaviour of some intelligent materials. It is developed by the LPMM.

Because of the recent leaving of several PhD students of the LAMAV laboratory previously involved in the development of Simula+, *a posteriori* error estimates functionalities should be from now developed in the GetFem++ software (author Yves Renard, INSA Lyon. GetFem++ is, like Simula+, a C++ library which allows the use of a vast choice of finite elements for 2D and 3D simulations, and which is based on a complete linear algebra library (GMM++). The connection of this code to the SIMPAF project also relies on the fact that it will allow to develop several *a posteriori* error estimators related to fluid-mechanics problems. Moreover, finite element and mesh functionalities will naturally be used in the codes developed by the project. It is already the case for the C++ code developped for the simulation of the low-Mach number flows (see section 3.4.4).

# 4.2. DDNS2

**Keywords:** 2D geometry, Domain Decomposition Methods, Dynamical Multi-Level Methods, Finite Elements Methods, Navier-Stokes, incompressible.

Participants: Caterina Calgaro [correspondant], Jacques Laminie.

The DDNS2 code is a parallel solver for unsteady incompressible Navier-Stokes flows in 2D geometries and primitive variables written in Fortran 95 with MPI as a message-passage library. Mixed finite element methods, with hierarchical basis, are used to discretize the equations and a non overlapping domain decomposition approach leads to an interface problem which involves a Lagrange multiplier corresponding to the velocity (the FETI approach). A dynamical multilevel method is developed locally on each subdomain. Several numerical estimates on the evolution of linear and nonlinear terms allow to construct the multilevel strategy which produces auto-adaptive cycles in time during which different mesh sizes, one for each subdomain, can be considered.

# 4.3. NS3ED

**Keywords:** *Exponential Mesh, Exterior Domains, Navier-Stokes, Preconditioning, Saddle-point Problems.* **Participants:** Caterina Calgaro [correspondant], Delphine Jennequin. The NS3ED code is a solver for steady incompressible Navier-Stokes flows in three-dimensional exterior domains, written in C++. The truncated problem is discretized using an exponential mesh and an equal-order velocity-pressure finite element method, with additional stabilization terms. A bloc-triangular preconditioner is performed for the generalized saddle-point problem.

# 4.4. NSVarDens

Keywords: Incompressible Navier-Stokes, Rayleigh-Taylor Instability, Variable Density.

Participants: Caterina Calgaro [correspondant], Emmanuel Creusé, Thierry Goudon, Emile Chane-Kane.

The NSVarDens code is based on a hybrid method coupling FV and FE approaches for solving the variable density Navier-Stokes equation in dimension 2. This original approach for variable density flows is described in [10]. The code, with a current version in Matlab, is still in a development phase, but simulations of the Rayleigh-Taylor instabilities prove the efficiency of the code. An optimized version will be produced soon and it will be completed by mesh refinements strategy.

# 4.5. RTcodes

Keywords: AP schemes, Radiative Transfer, Radiative shocks.

Participants: Pauline Lafitte [correspondant], Jean-François Coulombel, Christophe Besse, Thierry Goudon.

We have developed a set of numerical codes, written in Scilab, to compute the solutions of the system coupling the Euler equations to the radiation through energy exchanges, in the non equilibrium regime. This covers several situations in the hierarchy of asymptotic problems. The code treats the one-dimensional framework. In particular the code can be used to investigate radiative shocks profiles, as in e. g. [31]. The main advantage of our numerical codes is that they do not require any refinement near the singularities. The numerical tests show a very good agreement with the theoretical predictions.

# 4.6. FPcodes

Keywords: AP schemes, Fluid-Particles flows, Gravity driven flows.

Participants: Pauline Lafitte [correspondant], Thierry Goudon.

We have developed a numerical code, written in Scilab, to compute the solutions of the two-phase flows equations describing particles interacting with a fluid through friction forces. The code treats one-dimensional situation and is well adapted to describe gravity driven flows in either bubbling or flowing regimes. In particular, it can be used to describe the evolution of pollutants in the atmosphere. The numerical strategy, based on a asymptotic-based scheme, is described in details in [11].

# 4.7. CLAToolBox

Keywords: Absorbant boundary conditions, Schrödinger equation.

Participants: Christophe Besse [correspondant], Pauline Klein.

As a byproduct of the review paper [4], a user-friendly interface is offered<sup>5</sup> to trial and compare various numerical methods to solve the 1D Schrödinger equation with absorbant boundary conditions. We also mention [7] for a numerical investigation of blow-up phenomena in the nonlinear Schrödinger equation.

### 4.8. NLWcodes

Keywords: *Benjamin-Ono*, *Korteweg-de-Vries*, *nonlinear Schrödinger equations*. Participants: Caterina Calgaro [correspondant], Jean-Paul Chehab.

<sup>&</sup>lt;sup>5</sup>http://math.univ-lille1.fr/~besse/site/recherche/logiciels/index.html

We have developed a set of numerical codes, written in Matlab, to solve various 1D nonlinear wave equations (Korteweg-de-Vries, Benjamin-Ono, nonlinear Schrödinger), with or without damping term. These equations are discretized by pseudo-spectral or finite difference methods (compact schemes); a part of the corresponding study can be found in [26]. We compare the long time stability of various numerical methods and their capability to reproduce some physical invariants. These codes are still in development in order to simulate blow-up phenomena.

## 4.9. SPARCS

Keywords: Euler-Poisson system. Back-Trajectory method, Vlasov-Poisson system.

Participants: Christophe Besse, Thierry Goudon [correspondant], Nicolas Vauchelet, Ingrid Violet, Saja Borghol.

SPARCS is the code developped by Thales Alenia Space for the simulation of the charge phenomena the spacecrafts are subject to. The current version of the code, according to the PhD thesis of O. Chanrion and M. Chane-Yook performed in collaboration with the team Caiman at Sophia Antipolis, is specialized to geo-stationary atmospheres. The model consists in the stationary Vlasov-Poisson system, but where instationary effects are taken into account with the boundary condition for the electric field. We participate, in particular through the post doc of N. Vauchelet, to the elaboration of an improved version of the code which includes parallization optimized procedures, the modeling of the natural difference of potential between different dielectric surfaces of the spacecraft, as well as the possible presence of devices emitting charged particles. We aim at developing new versions designed for LEO and PEO atmospheres.

# 5. New Results

#### 5.1. Statistical Physics

The analysis of multi-scale phenomena and asymptotic problems aiming at identifying the influence of microscopic scales on the macroscopic observations is a hot topic in the team. Results have been obtained concerning the derivation of effective law describing the behavior of a particle interacting with a thermal bath or a set of oscillators. This work, which combines modeling efforts, analysis and large computations, is the object of a longstanding collaboration with P. Parris (Missouri-Rolla) see [18] and is the heart of the PhD thesis of B. Aguer. Some long time homogeneization of the effective behavior of related models has been obtained in [23], [33].

At the same time, M. Rousset is working on the numerical simulation of stochastically perturbed Molecular Dynamics. The main goal is to handle in the same simulation the fastest time scales (the oscillations of molecular bindings), and the slowest time scales (the so-called reaction coordinates). Adaptive methods are a popular tool to accelerate the slow time scales by using the appropriate bias which is computed "on-line". In [23] the long-time convergence analysis of the latter has been achieved. In [34], a new method has been proposed which drastically slow down the fast frequencies with a penalty and accelerates simulations, while conserving the statistical behavior of molecular systems.

# 5.2. Hyperbolic Problems, Conservation laws and Gas Dynamics

The convergence analysis of numerical schemes for conservation laws with unstructured meshes with an original proof based on probabilistic argument is a striking result due to F. Lagoutière with F. Delarue, [19]. More generally, we refer to [2] for an overview of F. Lagoutière's works.

The analysis of the stability of compressible vortex sheets has been carried out in [15] by J.-F. Coulombel. J.-F. Coulombel also studies the stability of finite difference approximation of hyperbolic problems with boundary conditions [29]. He generalizes and simplifies previous results by Gustaffson-Kreiss-Sundström. The analysis is a necessary starting point for extensions to multidimensional situations. J.-F. Coulombel has obtained a detailed description of the so-called hyperbolic region for hyperbolic boundary value problems [30]. This gives preliminary information in order to describe the propagation of high frequency signals and their reflection on the boundary. A synthetic survey of these results can be found on [1].

### 5.3. Computational Fluid Dynamics

We develop an original hybrid FV/FE<sup>6</sup> method to compute (2D) variable density viscous flows. The code allows to simulate complex phenomena like e. g. Rayleigh-Taylor instabilities [10]. We are also interested in the control of flows by active devices [16]. These questions naturally lead to investigate tools of numerical analysis like e.g. *a posteriori* estimators [17] or linear algebra problems [14]. In [27] C. Calgaro *et al.* address the problem of computing preconditioners for solving linear systems of equations with a sequence of slowly varying matrices. This problem arises in many important applications, for example in computational fluid dynamics, when the equations change only slightly possibly in some parts of the domain. In such situations, the papers discusses a number of techniques for computing incremental ILU factorizations.

### **5.4. Fluid/Particles Flows**

We are interested in two-phase flows involving a dense and a disperse phase. These models lead to interesting mathematical questions, [22]. We develop new asymptotic preserving methods for fluid/particles flows [11]. This approach follows the scheme we developed for radiative transfer equations [12].

#### **5.5. Plasmas Physics**

We obtained several results of asymptotic analysis concerning either kinetic or macroscopic models for charge transport, see [9], [8] and [13] (and we also refer to the related work [28]). Through the collaboration with Thales we participate to the development of Sparcs, a code of simulation for spacecraft electrical charge [25].

# 5.6. Artificial boundary conditions for the Schrödinger equations

The linear or nonlinear Schrödinger equation with potential is one of the basic equations of quantum mechanics and it arises in many areas of physical and technological interest, e.g. in quantum semiconductors, in electromagnetic wave propagation, and in seismic migration. The Schrödinger equation is the lowest order one-way approximation (paraxial wave equation) to the Helmholtz equation and is called Fresnel equation in optics, or standard parabolic equation in underwater acoustics. The solution of the equation is defined on an unbounded domain. If one wants to solve such a whole space evolution problem numerically, one has to restrict the computational domain by introducing artificial boundary conditions. So, the objective is to approximate the exact solution of the whole-space problem, restricted to a finite computational domain. A review article [4] was written this year to describe and compare the different current approaches of constructing and discretizing the transparent boundary conditions in one and two dimensions. However, these approaches are limited to the linear case (or nonlinear with the classical cubic nonlinearity: an article written was dedicated to this case this year [6]) and constant potentials. Therefore, in collaboration with X. Antoine (IECN Nancy and INRIA Lorraine), we proposed to P. Klein to study, in her PhD thesis, the case of the Schrödinger equation with variable potentials. The study of the non-stationary one-dimensional case has already led to one publication [5] and some preliminary results in the stationary case are really promising. These cases are relevant since for example the equations appear in the Bose Einstein condensate with a quadratic potential.

This problem is obviously not limited to the Schrödinger equation and new developments are in progress on the Korteweg de Vries equation with M. Ehrhardt. This equation is more difficult to study due to its third order derivative in space.

<sup>&</sup>lt;sup>6</sup>Finite Volume/Finite Element

### 5.7. Micro-macro models for rubber

In collaboration with R. Alicandro (U. of Cassino, Italy) and M. Cicalese (U. of Naples, Italy), A. Gloria has begun to address the derivation of rubber elasticity models from a discrete system of points in interaction, the system being described by a stochastic lattice. An article is in preparation. The asymptotic convergence of a finite element modeling of rubber introduced by Böl and Reese has been proved in [24]. With M. Vidrascu (project-team MACS) and P. Le Tallec (Ecole polytechnique), A. Gloria is currently working on the numerical simulation of the latter micro-macro model. Besides, M. Barchiesi (CNA, Pittsburgh, USA) and A. Gloria have found some new counterexamples to the cell formula in homogenization of nonlinear elasticity models, one of them being related to the discrete model. A preprint [35] has been submitted for publication.

### 5.8. Stochastic homogenization

A. Gloria has followed up on a work by X. Blanc, C. Le Bris (EPI MICMAC) and P.-L. Lions on a variant of stochastic homogenization. In particular, he has proved in [21] that for such a random structure a subadditive ergodic theorem still holds, which allows to generalize the homogenization results to the case of multiple integrals (and in particular nonlinear elasticity). Further results are the object of a collaboration with F. Otto (U. of Bonn, Germany) which started during A. Gloria's post-doc, and an article is currently in preparation. Moreover, A. Gloria has continued his study of numerical homogenization of elliptic PDEs, analyzing in [20] the method of windowing and oversampling used by practitioners (both in solid mechanics and flow in porous media).

# 6. Contracts and Grants with Industry

# 6.1. THALES

Participants: Christophe Besse, Thierry Goudon, Nicolas Vauchelet, Saja Borghol.

We started a new collaboration with Thales concerning the modelling and simulation of spacecraft/plasma interaction. The collaboration is the continuation of previous works performed in the project CAIMAN, at Sophia Antipolis (with S. Piperno, F. Poupaud, O. Chanrion, M. Chane-Yook). The goal is to develop the Thales code SPARCS which is designed to compute the electric potential on the spacecraft and around it. Of course, the motivation is to prevent possible failure of the spacecraft due to violent electric discharges. The current version of SPARCS, based on a back-trajectory method, is very efficient and provides an accurate computation of the potential and the distribution of charged particles on the surface. On the one hand, we try to fasten the computation by optimizing some procedures of the code and by proposing a parallel version. On the other hand, the current version of the code is specifically designed for GEO flights and our goal is to propose models and methods for treating different plasmas environments (LEO, PEO).

# 6.2. CEA

Participants: Thierry Goudon, Martin Parisot.

We are starting a collaborative program with the CEA (Direction des Applications Militaires) devoted to the modeling and simulation of plasmas arising in Inertial Confinement Fusion devices. We are concerned with the derivation of the so-called nonlocal models, which are variations around the standard diffusion models.

# 7. Other Grants and Activities

# 7.1. International Initiatives

### 7.1.1. ANR INTOCS

Participants: Pauline Lafitte, Jean-François Coulombel, Frédéric Lagoutière.

J.-F. Coulombel has obtained a 4-years ANR grant "young researcher", for the project INTOCS. In addition to the coordinator, two other members of the EPI SIMPAF are involved in this project: P. Lafitte et F. Lagoutière. The main scientific subject of the project is the interaction of compressible waves, and more precisely the propagation of high frequency oscillations in hyperbolic boundary value problems. One of the physical motivations is the "Mach stems" formation in reacting gas flows.

#### 7.1.2. ARC PANDA

Participants: Pauline Lafitte, Anne Devys, Thierry Goudon.

Some members of SIMPAF are involved in the ARC project PANDA, led by M. Doumic (EPI BANG, Rocquencourt); it is concerned with the theory and observations of polymerisation processes in prion and Alzheimer diseases. This research is connected to the PhD thesis of A. Devys, which is concerned with evolution problems in medecine and biology [32]. The project PANDA is currently under evaluation.

#### 7.1.3. AEN Fusion

Participants: Christophe Besse, Thierry Goudon.

SIMPAF is involved in the project led by E. Sonnendrucker from EPI Calvi, which aims at fostering the national research effort in mathematics and computer science towards the simulation of large magnetic confinement devices, like ITER. The project Fusion is currently under evaluation.

### 7.1.4. Project 3+3 "Méditerranée" MASOH

Participants: Jean-Paul Chehab, Christophe Besse, Caterina Calgaro, Olivier Goubet, Jacques Laminie, Thierry Goudon.

In 2006, under an initiative of J.-P. Chehab, the SIMPAF team has initiated a collaborating program "3+3 Méditerranée" funded by INRIA. This program is devoted to Modelling, Analysis and Simulation of Hydrodynamic Waves. To be more specific, the project focuses on water waves modelled by dispersive PDEs (Korteweg-De Vries, Benjamin-Ono, KP and Nonlinear Schrödinger equations). The goal is to elaborate efficient multilevel numerical schemes that will be able to help in the understanding of finite time blow up or the asymptotic smoothing effects due to damping. The project<sup>7</sup> brings together various collaborations the node of which is SIMPAF; the involved teams are

- France: SIMPAF, Amiens, Paris-Sud,
- Morocco : Marrakesh,
- Tunisia: Monastir,
- Spain: Granada.

As a consequence, four PhD theses were started co-advised by SIMPAF's members.

Emna Ezzoug, from Monastir, advised by E. Zahrouni, J. Laminie and O. Goubet, started in July 2006;

Ibtissem Damergi, from Monastir, by advised E. Zahrouni, Ch. Besse and O. Goubet, started in July 2006;

Salim Amr Salim Djabir, from Marrakesh, advised by M. Abounouh and J.-P. Chehab, started in January 2007;

Maithem Trabelsi, from Tunis advised by E. E. Zahrouni and J.-P. Chehab, started in September 2007.

In the context of the MASOH program, for research and teaching at the doctoral level, T. Goudon visited Granada; C. Calgaro, M. Abounouh, L. Di Menza, J.-P. Chehab visited the University of Monastir; while C. Calgaro, J.-P. Chehab, E. Zahrouni went to Marrakech. Besides, the PhD students spent a while in Amiens. The publications [3], [26] are directly related to interactions organized within this network.

<sup>&</sup>lt;sup>7</sup>described at the URL: http://math.univ-lille1.fr/~chehab/MASOH/masoh.html

# 8. Dissemination

# 8.1. Animation of the scientific community

- S. De Bièvre is a member of the scientific committee of the GDRE network "Mathematics and Quantum Physics" of the CNRS.
- T. Goudon is a member of the scientific committee of the CNRS European network GREFI-MEFI.
- T. Goudon and P. Lafitte are members of the Steering Committee of the Society of Industrial and Applied Math. (SMAI).
- T. Goudon is member of the "Conseil National des Universités" in the division of Applied Math.
- M. Rousset is involved in the organization of a HIM (Hausdorff Research Institute for Mathematics) Junior Trimester Program on Numerical methods in molecular simulation to be held in Bonn, February-April 2008.
- S. De Bièvre is invited to organize a session on "Quantum chaos" at the Mathematical Horizons for Quantum Physics programme of the Institute for Mathematical Sciences of the National University of Singapore in August 2008.
- The mathematics departments in the North area of France (namely from the Universities of Lille, Valenciennes, Calais, Amiens) decided some time ago to merge their efforts every year on specific topics and to organize jointly several events; 2008 has been specifically devoted to PDE and Numerical Analysis and our team has been involved in several scientific events:
  - Workshop "Open Dynamical Systems III", organized by J.-M. Bouclet, S. De Bièvre and M. Rousset, March 13-15 2008.
  - Workshop "9th IMACS International Symposium on Iterative Methods in Scientific Computing" organized by M. Bellalij, C. Calgaro, J.-P. Chehab, K. Jbilou and H. Sadok, held March 17-20, 2008, Lille.
  - Workshop "Finite Element and Finite Volume Methods in CFD", organized by P. Deuring, T. Goudon and S. Nicaise, held March 27-28, 2008.
  - Congrès National d'Analyse Numérique, a conference of the Society of Applied and Industrial Mathematics (SMAI), organized also with Univ. Paris 13, held May 26-30, 2008 at St Jean de Monts.
- C. Calgaro is in charge of the communication of the Math. Department and she is in charge of the relation between the University of Lille and High Schools. Accordingly, she organizes various events like "Les Métiers des math", the conference "Au-delà du compas"...

# 8.2. Teaching

- T. Goudon and P. Lafitte are members of the jury of the national hiring committee of the "Agrégation de mathématiques".
- S. De Bièvre is a member of the jury of the national hirring committee of the "CAPES de mathématiques".
- T. Goudon is in charge of the Doctoral formation in Applied Mathematics at the University of Lille.
- C. Besse and E. Creusé are involved in the project of a new International Master degree at the University of Lille devoted to Scientific Computing.
- Members of the team are involved in MSc degrees at USTL: J.-F. Coulombel, P. Lafitte give a course on the theory and the numerical treatment of conservation laws, S. De Bièvre offers a course on Hamiltonian mechanics, C. Calgaro and T. Goudon give a course on numerical methods for PDEs and E. Creusé makes a lecture on finite elements methods.

• Members of the team have been invited for lectures abroad: S. De Bièvre has been invited for lectures at the Chinese Academy of Sciences-Beijing, and at the CRM Montréal, Mc Gill whereas T. Goudon has been invited for a lecture on "Mathematical Models for Charge Transport" at University Fudan, Shanghai. C. Besse, C. Calgaro, J. P. Chehab, P. Lafitte made a series of courses either in the context of a Tempus program on numerical analysis or through the Masoh project.

# 9. Bibliography

# **Year Publications**

#### **Doctoral Dissertations and Habilitation Theses**

- [1] J.-F. COULOMBEL. Problèmes aux limites et problèmes asymptotiques dans l'étude des systèmes hyperboliques, Habilitation à Diriger des Recherches, Ph. D. Thesis, University Lille 1, 2008.
- [2] F. LAGOUTIÈRE. Analyse et approximation d'équations aux dérivées partielles en rapport avec la mécanique des fluides, Habilitation à Diriger des Recherches, Ph. D. Thesis, University Paris 7, 2008.

#### **Articles in International Peer-Reviewed Journal**

- [3] M. ABOUNOUH, H. AL MOATASSIME, J.-P. CHEHAB, S. DUMONT, O. GOUDET. Discrete Schrödinger Equations and dissipative dynamical systems, in "Comm. in Pure and Applied Analysis", vol. 7, n<sup>o</sup> 2, 2008, p. 211–227.
- [4] X. ANTOINE, A. ARNOLD, C. BESSE, M. EHRHARDT, A. SCHÄDLE. A Review of Transparent and Artificial Boundary Conditions Techniques for Linear and Nonlinear Schrödinger Equations, in "Communications in Computational Physics", vol. 4, 2008, p. 729–796.
- [5] X. ANTOINE, C. BESSE, P. KLEIN. Absorbing boundary conditions for the one-dimensional Schrödinger equation with an exterior repulsive potential, in "Journal of Computational Physics", to appear, 2008.
- [6] X. ANTOINE, C. BESSE, J. SZEFTEL. *Towards accurate artificial boundary conditions for nonlinear PDEs through examples*, in "Cubo A Mathematical Journal", to appear, 2008.
- [7] C. BESSE, R. CARLES, N. MAUSER, H.-P. STIMMING. Monotonicity properties of blow-up time for nonlinear Schrödinger equation: numerical tests, in "Discrete and Cont. Dyn. Syst. B", vol. 9, 2008, p. 11–36.
- [8] M. BOSTAN, T. GOUDON. *High-electric-field limit for the Vlasov-Maxwell-Fokker-Planck system*, in "Ann. IHP Non Linear Anal.", vol. 25, 2008, p. 1221–1251.
- [9] M. BOSTAN, T. GOUDON. Low field regime for the relativistic Vlasov-Maxwell-Fokker-Planck system; the one and one half dimensional case, in "AIMS-Kinetic Related Models", vol. 1, 2008, p. 139-169.
- [10] C. CALGARO, E. CREUSÉ, T. GOUDON. A hybrid finite volume-finite elements method for variable density incompressible flows, in "Journal of Computational Physics", vol. 227, n<sup>o</sup> 9, 2008, p. 4671-4696.
- [11] J. A. CARRILLO, T. GOUDON, P. LAFITTE. Simulation of Fluid & Particles Flows: Asymptotic Preserving Schemes for Bubbling and Flowing Regimes, in "J. Comp. Phys.", vol. 227, 2008, p. 7929–7951.

- [12] J. A. CARRILLO, T. GOUDON, P. LAFITTE, F. VECIL. Numerical schemes of diffusion asymptotics and moment closures for kinetic equations, in "J. Sci. Comput.", vol. 35, 2008, p. 113-149.
- [13] C. CHAINAIS, Y.-J. PENG, I. VIOLET. Numerical solutions of the Euler-Poisson systems for the potential flows, in "Applied numerical mathematics (APNUM)", vol. 59, 2009, p. 301-315.
- [14] J.-P. CHEHAB, M. RAYDAN. Geometrical properties of the Frobenius condition number for positive definite matrices, in "Linear Algebra and its Appl.", 2008.
- [15] J.-F. COULOMBEL. Nonlinear compressible vortex sheets in two space dimensions, in "Ann. Sci. École Norm. Sup. (4)", vol. 41, n<sup>o</sup> 1, 2008, p. 85–139.
- [16] E. CREUSÉ, A. GIOVANNINI, I. MORTAZAVI. Vortex simulation of active control strategies for transitional backward-facing step flows, in "Computers and Fluids", vol. In Press, 2008.
- [17] E. CREUSÉ, S. NICAISE. A posteriori error estimations of a coupled mixed and standard Galerkin method for second order operators, in "J. Comput. Appl. Math.", vol. 213, n<sup>o</sup> 1, 2008, p. 35-55.
- [18] S. DE BIÈVRE, P. LAFITTE, P. PARRIS. Normal transport properties for a classical particle coupled to a non-Ohmic bath, in "Journal of Statistical Physics", to appear, 2008.
- [19] F. DELARUE, F. LAGOUTIÈRE. Probabilistic Analysis of the Upwind Scheme for Transport, in "Arch. Ration. Mech. Anal.", to appear, 2008.
- [20] A. GLORIA. An analytical framework for numerical homogenization Part II: windowing and oversampling, in "Multiscale Model. Simul.", vol. 7, n<sup>o</sup> 1, 2008, p. 275–293.
- [21] A. GLORIA. *Stochastic diffeomorphisms and homogenization of multiple integrals*, in "Applied Math. Res. Expr.", Article ID abn001, 2008.
- [22] F. LAGOUTIÈRE, N. SEGUIN, N. TAKAHASHI. A simple 1D model of inviscid fluid-solid interaction, in "J. Differential Equations", to appear, 2008.
- [23] T. LELIÈVRE, M. ROUSSET, G. STOLTZ. Long-time convergence of an Adaptive Biasing Force method, in "Nonlinearity", vol. 21, 2008, p. 1155-1181.

#### **International Peer-Reviewed Conference/Proceedings**

[24] R. ALICANDRO, M. CICALESE, A. GLORIA. Convergence analysis of the Böl-Reese discrete model for rubber, in "Proceedings of the 11th International Symposium on Continuum Models and Discrete Systems", 2008.

#### **Research Reports**

- [25] C. BESSE, J.-P. DUDON, T. GOUDON, N. VAUCHELET. Comparison of Vlasov solvers for spacecraft charging simulation, Preprint, Technical report, INRIA, 2008.
- [26] C. CALGARO, J.-P. CHEHAB, J. LAMINIE, E. ZAHROUNI. Schémas multiniveaux pour les équations d'ondes en dimension 1, rapport-00271154, Technical report, INRIA, 2008, http://hal.inria.fr/inria-00271154/fr/.

- [27] C. CALGARO, J.-P. CHEHAB, Y. SAAD. Incremental Incomplete LU factorizations with applications to timedependent PDEs, Technical report, preprint, 2008.
- [28] C. CHAINAIS, I. VIOLET. Existence of solutions to a corrosion model, Technical report, 2008.
- [29] J.-F. COULOMBEL. Stability of finite difference schemes for hyperbolic initial boundary value problems, Technical report, 2008.
- [30] J.-F. COULOMBEL. The hyperbolic region for hyperbolic boundary value problems, Technical report, 2008.
- [31] J.-F. COULOMBEL, P. LAFITTE. Computation of shock profiles in radiative hydrodynamics, Preprint, Technical report, INRIA, 2008.
- [32] A. DEVYS, T. GOUDON, P. LAFITTE. A model describing the growth and the size distribution of multiple metastatic tumors, Preprint, Technical report, INRIA, 2008.
- [33] T. GOUDON, M. ROUSSET. *Stochastic acceleration in an inhomogenous time random force field*, Preprint, Technical report, INRIA, 2008.
- [34] P. PLECHAC, M. ROUSSET. Exact and non-stiff sampling of highly oscillatory systems with implicit massmatrix penalization, Technical report, 2008.

#### **Other Publications**

[35] M. BARCHIESI, A. GLORIA. New counterexamples to the cell formula in nonconvex homogenization, 2008, http://math.sns.it/cgi/get.cgi/papers/barglo08/AntMar.pdf.