

INSTITUT NATIONAL DE RECHERCHE EN INFORMATIQUE ET EN AUTOMATIQUE

Project-Team FLUMINANCE

Fluid flow Analysis, Description and Control from Image Sequences

Rennes - Bretagne-Atlantique



Theme : Observation and Modeling for Environmental Sciences

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2. Overall Objectives

2.1. Overall Objectives

The research group that we have entitled FLUMINANCE from a contraction between the words "Fluid" and "Luminance" is dedicated to the extraction of information on fluid flows from image sequences and to the development of tools for the analysis and control of these flows. The objectives of the group are at the frontiers of several important domains. The group aims at providing in the one hand image sequence methods devoted to the analysis and description of fluid flows and in the other hand physically consistent models and operational tools to extract meaningful features characterizing or describing the observed flow and enabling decisions or actions. Such a twofold goal is of major interest for the inspection, the analysis and the monitoring of complex fluid flows, but also for control purpose of specific flows involved in industrial problems. To reach these goals we will mainly rely on data assimilation strategies and on motion measurement techniques. From a methodological point of view, the techniques involved for image analysis are either stochastic or variational. One of the main originality of the the FLUMINANCE group is to combine cutting-edge researches on these methods with an ability to conduct proper intensive experimental validations on prototype flows mastered in laboratory. The scientific objectives decompose in three main themes:

• Characterization of fluid flow from images

We aim here at providing accurate measurements and consistent analysis of complex fluid flows through image analysis techniques. The application domain ranges here from industrial processes and experimental fluid mechanics to environmental and life sciences. This theme includes also the use of non-conventional imaging techniques such as Schlieren techniques, Shadowgraphs, holography. The objective will be here to go towards 3D dense velocity measurements.

Coupling dynamical model and image data

We focus here on the study, through image data, of complex and partially known fluid flows involving complex boundary conditions, multi-phase fluids, fluids and structures interaction problems. Our credo is that image analysis can provide sufficiently fine observations on small an medium scales to construct models which, applied at medium and large scale, account accurately for a wider range of the dynamics scales. The image data and a sound modeling of the dynamical uncertainty at the observation scale should allow us to reconstruct the observed flow and to provide efficient real flows (experimental or natural) based dynamical modeling. Our final goal will be to go towards a 3D reconstruction of real flows, or to operate large motion scales simulations that fit real world flow data and incorporate an appropriate uncertainty modeling.

• Control and optimization of turbulent flows

We are interested here on active control and more precisely on closed-loop control. The main idea is to extract reliable image features to act on the flow. This approach is well known in the robot control community, it is called visual servoing. More generally, it is a technique to control a dynamic system from image features. We plan to apply this approach on flows involved in various domains such as environment, transport, microfluidic, industrial chemistry, pharmacy, food industry, agriculture, etc.

3. Scientific Foundations

3.1. Fluid flow analysis and modeling

Turbulent fluid flows involved in environmental or industrial applications are complex. In fluid mechanics laboratories, canonical turbulent shear flows have been studied for many years and a relatively clear picture of their underlying structure exists. However, the direct applicability of these efforts to real relevant flows, which often occur in complex geometries and in the presence of multiple non canonical influences, like cross-shear, span wise non-uniform and thermal stratification, is still unknown. In addition, the turbulence can be characterized by Reynolds number ranging between 10^3 and 10^4 , corresponding to transitional regime for which the use of classical turbulence models is limited.

In this context, we have performed research studies on turbulent shear flows of low velocities by tackling crucial topics of measurements, analysis and modeling of environmental and industrial flows in presence of non-canonical influences. This concerns more precisely the study of the interaction between a mixing layer and circular cylinder wake flow, the study of wake flow with span wise non uniformity, the study of mixing layer under the influence of thermal stratification and the study of mixing layer forced between non-uniform flows. The analysis of these flows has required the design of adequate dynamical models, using proper orthogonal decomposition and Galerkin projection. Understanding issues such as the mechanisms of heat and mass transfer involved in these shear flows provides meaningful information for the control of relevant engineering flows and the design of new technologies. To investigate more thoroughly these complex flows numerical and experimental tools have been designed. An immersed boundary method was proposed to mimic complex geometries into Direct Numerical simulation (DNS) and Large Eddy Simulations (LES) codes. A novel anemometer has been designed and implemented for the simultaneous measurement of velocity and temperature in air flows with a single hot-wire probe.

Mixing layer wake interaction

We have investigated the vortex shedding of a circular cylinder immersed in a plane turbulent mixing layer. For a centre span Reynolds number of 7500, the wake flow splits into three regions: a high-velocity wake, a low-velocity wake and a region of interaction in the middle span of the body. A strong unsteady secondary flow is observed, and explained with span wise base pressure gradients. Unexpected features are found for formation length and the base pressure along the span of the cylinder. In the high-velocity side, where the local Reynolds number is the highest, the formation length is longest. Based on the formation length measurements it was shown that as a function of the centre span Reynolds number, the wake flows behaves as circular cylinder in uniform flow. Three cells with a constant frequency with adjacent dislocations are observed. For each cell, a shedding mode was suggested. The relation of the secondary flow to the frequencies was examined. All the observations were analyzed by analogical reasoning with other flows. This pointed out the action of the secondary flow in the high-velocity side regarded as a wake interference mechanism [26].

Low order complex flow modeling

We have proposed improvements to the construction of low order dynamical systems (lods) for incompressible turbulent external flows. The reduced model is obtained by means of a Proper Orthogonal Decomposition (pod) basis extracted through a truncated singular value decomposition of the flow auto-correlation matrix built from noisy PIV experimental velocity measurements. The POD modes are then used to formulate a reduced dynamical system that contains the main features of the flow. This low order dynamical system (LODS) is obtained through a Galerkin projection of the Navier-Stokes Equations on the POD basis. Usually, the resulting system of ordinary differential equations presents stability problems due to modes truncation and numerical uncertainties, especially when working on experimental data. The technique we proposed relies on an optimal control approach to estimate the dynamical system coefficients and its initial condition. This allows us to recover a reliable and stable spatio-temporal reconstruction of the large scales of the flow. The technique has been assessed on the near wake behind a cylinder observed through very noisy PIV measurement. It has been also evaluated for configurations involving a rotating cylinder.

Studies on complex 3D dynamical behavior resulting from the interaction between a plane mixing layer and the wake of a cylinder have been also investigated using POD representation, applied to data from two synchronized 2D PIV systems (Dual-plane PIV). This approach allowed us to construct a 3D-POD representation. An analysis of the correlations shows different length scales in the regions dominated by wake like structures and shear layer type structures [18]. In order to characterize the particular organization in the plane of symmetry, a Galerkin projection from a slice POD has been performed. This led to a low-dimensional dynamical system that allowed the analysis of the relationship between the dominant frequencies. This study led to a reconstruction of the dominant periodic motion suspected from previous studies [17]. This work allowed us to make a link between the three-dimensional organization and the secondary unsteady motion from the low velocity side to the high velocity side of the mixing layer, appearing in this highly 3D flow configuration.

Direct and Large Eddy simulations of complex flows

During the PhD of P. Parnaudeau, we have proposed a direct forcing method better suited to the use of compact finite difference schemes in Direct Numerical Simulation. The new forcing creates inside the body an artificial flow preserving the no-slip condition at the surface but reducing the step-like change of the velocity derivatives across the immersed boundary. This modification led to improve results both qualitatively and quantitatively for conventional and complex flow geometries [35].

Three-dimensional direct numerical simulations have been performed for vortex shedding behind cylinders. We focused in particular on cases for which the body diameter and the incoming flow involved span wise linear non-uniformity. Four configurations were considered: the shear flow, the tapered cylinder and their combinations, which gave rise namely to the adverse and aiding cases. In contrast with the observations of other investigators, these computations highlighted distinct vortical features between the shear case and the tapered case. In addition, it was observed that the shear case and the adverse case (respectively the tapered and aiding case), yielded similarities in flow topology. This phenomenon was explained by the span wise variations of the ratio of mean velocity and the cylinder diameter which seemed to govern these flows. Indeed, it was observed that large span wise variations of U/D seemed to enhance three-dimensionality, through the

appearance of vortex-adhesions and dislocations. Span wise cellular pattern of vortex shedding were identified. Their modifications in cell size, junction position and number were correlated with the variation of U/D. In the Lee side of the obstacle a wavy secondary motion was identified. Induced secondary flow due to the bending of Karman vortices in the vicinity of vortex-adhesion and dislocations was suggested to explain this result [34].

LES and experimental wake flow database

We contributed to the study of flow over a circular cylinder at Reynolds number Re = 3900. Although this classical flow is widely documented in the literature, especially for this precise Reynolds number, which leads to a sub critical flow regime, there is no consensus about the turbulence statistics immediately just behind the obstacle. This flow has been studied both numerically with Large Eddy Simulation and experimentally with Hot-Wire Anemometry and Particle Image Velocimetry. The numerical simulation has been performed using high-order schemes and the specific Immersed Boundary Method previously mentioned. We focused on turbulence statistics and power spectra in the near wake up to 10 diameters. Statistical estimation is shown to need large integration times increasing the computational cost and leading to an uncertainty of about 10% for most flow characteristics considered in this study. The present numerical and experimental results are found to be in good agreement with previous Large Eddy Simulation data. Our study has exhibited significant differences compared with the experimental data found in the literature. The obtained results attenuate previous numerical-experimental controversy for this type of flows [33].

Simultaneous velocity temperature measurements in turbulent flows

We have worked on the design of a novel anemometer for the simultaneous measurement of velocity and temperature in airflows with a single hot wire probe. The principle of periodically varying the overheat ratio of the wire has been selected and applied through a tunable electronic chain. Specific methods were developed for the calibration procedure and the signal processing. The accuracy of the measurements was assessed by means of Monte-Carlo simulations. Accurate results were provided for two types of turbulent non-isothermal flows, a coaxial heated jet and a low speed thermal mixing. The particular interest of the synchronization of the two measurements has been emphasized during the PhD thesis of T. Ndoye.

A new dynamic calibration technique has been developed for hot-wire probes. The technique permits, in a short time range, the combined calibration of velocity, temperature and direction calibration of single and multiple hot-wire probes. The calibration and measurements uncertainties were modeled, simulated and controlled, in order to reduce their estimated values.

3.2. Fluid motion analysis

Flow visualization has been a powerful tool to depict or to understand flow feature properties. Efforts to develop high-quality flow visualization techniques date back over a century. The analysis of the recorded images consisted firstly to a qualitative interpretation of the streak lines leading to an overall global insight into the flow properties but lacking quantitative details on important parameters such as velocity fields or turbulence intensities. Point measurement tools such as hot wire probes or Laser Doppler Velocimetry have typically provided these details. As these probes give information only at the point where they are placed, simultaneous evaluations at different points require to dispose a very large number of probes and the evaluation of unsteady field (most of the flows are unsteady) is almost unachievable with them.

In an effort to avoid the limitations of these probes, the Particle Image Velocimetry (PIV), a non-intrusive diagnostic technique, has been developed in the last two decades [14]. The PIV technique enables obtaining velocity fields by seeding the flow with particles (e.g. dye, smoke, particles) and observing the motion of these tracers. In computer vision, the estimation of the projection of the apparent motion of a 3D scene onto the image plane, refereed in the literature as optical-flow, is an intensive subject of researches since the 80's and the seminal work of B. Horn and B. Schunk [28]. Unlike to dense optical flow estimators, the former approach provides techniques that supply only sparse velocity fields. These methods have demonstrated to be robust and to provide accurate measurements for flows seeded with particles. These restrictions and their inherent discrete local nature limit too much their use and prevent any evolutions of these techniques towards the devising of methods supplying physically consistent results and small scale velocity measurements. It does

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not authorize also the use of scalar images exploited in numerous situations to visualize flows (image showing the diffusion of a scalar such as dye, pollutant, light index refraction, flurocein,...). At the opposite, variational techniques enable in a well-established mathematical framework to estimate spatially continuous velocity fields, which should allow more properly to go towards the measurement of smaller motion scales. As these methods are defined through PDE's systems they allow quite naturally including as constraints the kinematical and dynamical laws governing the observed fluid flows. Besides, within this framework it is also much easier to define characteristic features estimation on the basis of physically grounded data model that describes the relation linking the observed luminance function and some state variables of the observed flow. This route has demonstrated to be much more robust to scalar image. Several studies in this vein have strengthened our skills in this domain. All the following approaches have been either formulated within a statistical Markov Random Fields modeling or either within a variational framework. For a thorough description of these approaches see [27].

ICE data model and div-curl regularization This fluid motion estimator has been developed during the PhD thesis of Thomas Corpetti. It is constructed on a data model derived from the Integration of the Continuity Equation (ICE data model) and includes a second order regularization scheme enabling to preserve blobs of divergence and curl. Intensive evaluations of this estimator on flow prototypes mastered in laboratory have shown that this estimator led to the same order of accuracy as the best PIV techniques but for an increase information density. This ability to get dense flow fields allowed us estimating proper vorticity or divergence maps without resorting to additional post-processing interpolation schemes.

Schlieren Image velocimetry We have addressed the problem of estimating the motion of fluid flows visualized with the Schlieren technique. Such an experimental visualization system is well known in fluid mechanics and it enables the visualization of unseeded flows. This technique authorizes the capture of phenomena that are impossible to visualize with particle seeding such as natural convection, phonation flow, breath flow and allows the setting of large scale experiments. Since the resulting images exhibit very low intensity contrasts, classical motion estimation methods based on the brightness constancy assumption (correlation-based approaches, optical flow methods) are completely inefficient. The global energy function we have defined for Schlieren images is composed of i) a specific data model accounting for the fact that the observed luminance is related to the gradient of the fluid density, and ii) a specific constrained div-curl regularization term. To date there exists no motion estimator allowing estimating accurately dense velocity fields on Schlieren images.

Low order fluid motion estimator During the PhD of Anne Cuzol, we have worked on the definition of a low-dimensional fluid motion estimator. This estimator is based on the Helmholtz decomposition, which consists in representing the velocity field as the sum of a divergence-free component and a curl-free one. In order to provide a low-dimensional solution, both components have been approximated using a discretization of the vorticity (curl of the velocity vector) and divergence maps through regularized Dirac measures [23]. The resulting so-called irrotational (resp. solenoidal) field is then represented by a linear combination of basis functions obtained by a convolution product of the Green kernel gradient and the vorticity map (resp. the divergence map). The coefficient values and the basis function parameters are obtained by minimizing a function formed by an integrated version of the mass conservation principle of fluid mechanics.

Potential functions estimation and finite mimetic differences In collaboration with the Mannheim University and the group of C. Schnoerr, we have studied a direct estimation approach of the flow potential functions (respectively the *stream* function and the *velocity* potential) from two consecutive images. The estimation has been defined on the basis of a high order regularization scheme and has been implemented through mimetic difference methods. With these approaches the discretization preserves basic relationships of continuous vector analysis. Compared to previous discretization scheme based on auxiliary div-curl variables, the considered technique appeared to be numerically much more stable and led to an improve accuracy.

2D and 3D atmospheric motion layer estimation In this study, we have explored the problem of estimating mesoscales dynamics of atmospheric layers from satellite image sequences. Due to the intrinsic sparse 3-dimensional nature of clouds and to large occluded zones caused by the successive overlapping of cloud layers, the estimation of accurate layered dense motion fields is an intricate issue. Relying on a physically

sound vertical decomposition of the atmosphere into layers, we have proposed two dense motion estimators for the extraction of multi-layer horizontal (2D) and 3D wind fields. These estimators are expressed as the minimization of a global function that includes a data-driven term and a spatio-temporal smoothness term. A robust data term relying on shallow-water mass conservation model has been proposed to fit sparse observations related to each layer. In the 3D case, the layers are interconnected through a term modeling mass exchanges at the layers surfaces frontiers.

A novel spatio-temporal regularizer derived from the shallow-water momentum conservation model has been considered to enforce temporal consistency of the solution along time. These constraints are combined with a robust second-order regularizer preserving divergent and vorticity structures of the flow. Besides, a two-level motion estimation scheme has been settled to overcome the limitations of the multiresolution incremental estimation scheme when capturing the dynamics of fine mesoscale structures. This alternative approach relies on the combination of correlation and optical-flow observations. An exhaustive evaluation of the novel method has been first performed on a scalar image sequence generated by Direct Numerical Simulation of a turbulent bi-dimensional flow. Based on qualitative experimental comparisons, the method has also been assessed on a Meteosat infrared image sequence.

3.3. Data assimilation and Tracking of characteristic fluid features

Classical motion estimation techniques usually proceed on pairs of two successive images, and do not enforce temporal consistency. This often induces an estimation drift which is essentially due to the fact that motion estimation is formulated as a local process in time. No adequate physical dynamics law, or conservation law, related to the observed flow, is taken into account over long time intervals by the usual motion estimators. The estimation of an unknown state variable trajectory on the basis of specified dynamical laws and some incomplete and noisy measurements of the variable of interest can be either conducted through optimal control techniques or through stochastic filtering approach. These two frameworks have their own advantages and deficiencies. We rely indifferently on both approaches.

Stochastic filtering for fluid motion tracking We have proposed a recursive Bayesian filter for tracking velocity fields of fluid flows. The filter combines an Îto diffusion process associated to 2D vorticity-velocity formulation of Navier-Stokes equation and discrete image error reconstruction measurements. In contrast to usual filters, designed for visual tracking problem, our filter combines a continuous law for the description of the vorticity evolution with discrete image measurements. We resort to a Monte-Carlo approximation based on particle filtering. The designed tracker provides a robust and consistent estimation of instantaneous motion fields along the whole image sequence. In order to handle a state space of reasonable dimension for the stochastic filtering problem, the motion field is represented as a combination of adapted basis functions. The basis functions are derived from a mollification of Biot-Savart integral and a discretization of the vorticity and divergence maps of the fluid vector field. The output of such a tracking is a set of motion fields along the whole time range of the image sequence. As the time discretization is much finer than the frame rate, the method provides consistent motion interpolation between consecutive frames. In order to reduce further the dimensionality of the associated state space when we are facing a large number of motion basis functions, we have explored a new dimensional reduction approach based on dynamical systems theory. The study of the stable and unstable directions of the continuous dynamics enables to construct an adaptive dimension reduction procedure. It consists in sampling only in the unstable directions, while the stable ones are treated deterministically [24].

When the likelihood of the measurement can be modeled as Gaussian law, we have also investigated the use of so-called ensemble Kalman filtering for fluid tracking problems. This kind of filters introduced for the analysis of geophysical fluids is based on the Kalman filter update equation. Nevertheless, unlike traditional Kalman filtering setting, the covariances of the estimation errors, required to compute the Kalman gain, rely on an ensemble of forecasts. Such a process gives rise to a Monte Carlo approximation for a family of stochastic non linear filters enabling to handle state spaces of large dimension. We have recently proposed an extension of this technique that combines sequential importance sampling and the propagation law of ensemble kalman filter. This technique leads to ensemble Kalman filter with an improve efficiency. This appears to be a generalization

of the optimal importance sampling strategy we proposed in the context of partial conditional Gaussian trackers [15], [16].

Variational assimilation technique

We investigated the use of variational framework for the tracking from image sequence of features belonging to high dimensional spaces. This framework relies on optimal control principles as developed in environmental sciences to analyze geophysical flows [25], [29]. Within the PhD of Nicolas Papadakis [31], [32], we have first devised a data assimilation technique for the tracking of closed curves and their associated motion fields. The proposed approach enables a continuous tracking along an image sequence of both a deformable curve and its associated velocity field. Such an approach has been formalized through the minimization of a global spatio-temporal continuous cost functional, with respect to a set of variables representing the curve and its related motion field. The resulting minimization sequence consists in a forward integration of an evolution law followed by a backward integration of an adjoint evolution model. The latter pde includes a term related to the discrepancy between the state variables evolution law and discrete noisy measurements of the system. The closed curves are represented through implicit surface modeling [30], whereas the motion is described either by a vector field or through vorticity and divergence maps according to the type of targeted application. The efficiency of the approach has been demonstrated on two types of image sequences showing deformable objects and fluid motions.

More recently assimilation technique for the direct estimation of atmospheric wind field from pressure images have been proposed [22]. These techniques rely on a brightness variation model of the intensity function. They do not include anymore motion measurements provided by external motion estimators. The resulting estimator allows us to recover accurate fluid motion fields and enables tracking dense vorticity maps along an image sequence.

3.4. Visual servoing

Nowadays, visual servoing is a widely used technique is robot control. It consists in using data provided by a vision sensor for controlling the motions of a robot [19]. Various sensors can be considered such as perspective cameras, omnidirectional cameras, 2D ultrasound probes or even virtual cameras. In fact, this technique is historically embedded in the larger domain of sensor-based control [36] so that other sensors than vision sensors can be properly used. On the other hand, this approach was first dedicated to robot arms control. Today, much more complex system can be considered like humanoid robots, cars, submarines, airships, helicopters, aircrafts. Therefore, visual servoing is now seen as a powerful approach to control the state of dynamic systems.

Classically, to achieve a visual servoing task, a set of visual features s has to be selected from visual measurements m extracted from the image. A control law is then designed so that these visual features reach a desired value s^{*} related to the desired state of the system. The control principle is thus to regulate to zero the error vector $\mathbf{e} = \mathbf{s} - \mathbf{s}^*$. To build the control law, the knowledge of the so-called *interaction matrix* \mathbf{L}_s is usually required. This matrix links the time variation of s to the camera instantaneous velocity v

$$\dot{\mathbf{s}} = \mathbf{L}_{\mathbf{s}} \, \mathbf{v} + \frac{\partial \mathbf{s}}{\partial t} \tag{1}$$

where the term $\frac{\partial s}{\partial t}$ describes the non-stationary behavior of s. Typically, if we try to ensure an exponential decoupled decrease of the error signal and if we consider the camera velocity as the input of the robot controller, the control law writes as follow

$$\mathbf{v} = -\lambda \widehat{\mathbf{L}_{\mathbf{s}}}^{+} \mathbf{e} - \widehat{\mathbf{L}_{\mathbf{s}}}^{+} \frac{\partial \widehat{\mathbf{e}}}{\partial t}$$
(2)

with λ a proportional gain that has to be tuned to minimize the time-to-convergence, $\widehat{\mathbf{L}_s}^+$ the pseudo-inverse of a model or an approximation of \mathbf{L}_s and $\frac{\partial \mathbf{\hat{e}}}{\partial t}$ an estimation of $\frac{\partial \mathbf{e}}{\partial t}$.

The behavior of the closed-loop system is then obtained, from (2), by expressing the time variation of the error e

$$\dot{\mathbf{e}} = -\lambda \mathbf{L}_{\mathbf{s}} \widehat{\mathbf{L}}_{\mathbf{s}}^{+} \mathbf{e} - \mathbf{L}_{\mathbf{s}} \widehat{\mathbf{L}}_{\mathbf{e}}^{+} \frac{\partial \mathbf{e}}{\partial t} + \frac{\partial \mathbf{e}}{\partial t}.$$
(3)

As can be seen, visual servoing explicitly relies on the choice of the visual features s and then on the related interaction matrix; that is the key point of this approach. Indeed, this choice must be performed very carefully. Especially, an isomorphism between the camera pose and the visual features is required to ensure that the convergence of the control law will lead to the desired state of the system. An optimal choice would result in finding visual features leading to a diagonal and constant interaction matrix and, consequently, to a linear decoupled system for which the control problem is well known. Thereafter, the isomorphism as well as the global stability would be guaranteed. In addition, since the interaction matrix would present no more nonlinearities, a suitable robot trajectory would be ensured.

However, finding such visual features is a very complex problem and it is still an open issue. Basically, this problem consists in building the visual features s from the nonlinear visual measurements m so that the interaction matrix related to s becomes diagonal and constant or, at least, as simple as possible.

On the other hand, a robust extraction, matching (between the initial and desired measurements) and realtime spatio-temporal tracking (between successive measurements) have to be ensure but have proved to be a complex task, as testified by the abundant literature on the subject. Nevertheless, this image process is, to date, a necessary step and often considered as one of the bottlenecks of the expansion of visual servoing. That is why more and more non geometric visual measurements are proposed [20].

4. Application Domains

4.1. Application Domains

By designing new approaches for the analysis of fluid-image sequences the FLUMINANCE group aims at contributing to several application domains of great interest for the community and in which the analysis of complex fluid flows plays a central role. The group focuses mainly on two broad applications domain:

- Environmental sciences;
- Experimental fluid mechanics and industrial flows.

4.1.1. Environmental sciences

The first huge application domain concerns all the sciences that aim at observing the biosphere evolution such as meteorology, climatology or oceanography but also remote sensing study for the monitoring of meteorological events or human activities consequences. For all these domains image analysis is a practical and unique tool to *observe, detect, measure, characterize or analyze* the evolution of physical parameters over a large domain. The design of generic image processing technique for all these domains might offer practical software tools to measure precisely the evolution of fluid flows for weather forecasting or climatology studies. It might also offer possibilities of closed surveillance of human and natural activities in sensible areas such as forests, river edges, and valley in order to monitor pollution, floods or fire. The need in term of local weather forecasting, risk prevention, or local climate change is becoming crucial for our tomorrow's life. At a more local scale, image sensors may also be of major utility to analyze precisely the effect of air curtains for safe packaging in agro-industrial.

4.1.2. Experimental fluid mechanics and industrial flows

In the domain of **experimental fluid mechanics**, the visualization of fluid flows plays a major role, especially for turbulence study since high frequency imaging has been made currently available. Together with analysis of turbulence at different scales, one of the major goals pursued at the moment by lot of scientists and engineers consists in studying the ability to manipulate a flow to induce a desired change. This is of huge technological importance to enhance or inhibit mixing in shear flows, improve energetic efficiency or control the physical effects of strain and stresses. This is for instance of particular interest for:

- Military applications, for example to limit the infra-red signatures of fighter aircraft;
- Aeronautics and transportation, to limit fuel consumption by controlling drag and lift effects of turbulence and boundary layer behavior;
- Industrial applications, for example to monitor flowing, melting, mixing or swelling of processed materials, or preserve manufactured products from contamination by airborne pollutants, or in industrial chemistry to increase chemical reactions by acting on turbulence phenomena.

5. Software

5.1. DenseMotion software - Estimation of 2D dense motion fields

Participants: Thomas Corpetti, Patrick Héas, Etienne Mémin.

This code allows the computation from two consecutive images of a dense motion field. The estimator is expressed as a global energy function minimization. The code enables the choice of different data model and different regularization functional depending on the targeted application. Generic motion estimator for video sequences or dedicated motion estimator for fluid flows can be specified. This estimator allows in addition the users to specify additional correlation based matching measurements. It enables also the inclusion of a temporal smoothing prior relying on a velocity vorticity formulation of the Navier-Stoke equation for Fluid motion analysis applications. The different variants of this code correspond to research studies that have been published in IEEE transaction on Pattern Analysis and machine Intelligence, Experiments in Fluids, IEEE transaction on Image Processing, IEEE transaction on Geo-Science end Remote Sensing. The binary of this code can be freely downloaded on the FLUID web site http://fluid.irisa.fr.

5.2. 2DLayeredMotion software - Estimation of 2D independent mesoscale layered atmospheric motion fields

Participants: Patrick Héas, Etienne Mémin, Nicolas Papadakis.

This software enables to estimate a stack of 2D horizontal wind fields corresponding to a mesoscale dynamics of atmospheric pressure layers. This estimator is formulated as the minimization of a global energy function. It relies on a vertical decomposition of the atmosphere into pressure layers. This estimator uses pressure data and classification clouds maps and top of clouds pressure maps (or infra-red images). All these images are routinely supplied by the EUMETSAT consortium which handles the Meteosat and MSG satellite data distribution. The energy function relies on a data model built from the integration of the mass conservation on each layer. The estimator also includes a simplified and filtered shallow water dynamical model as temporal smoother and second-order div-curl spatial regularizer. The estimator may also incorporate correlation-based vector fields as additional observations. These correlation vectors are also routinely provided by the Eumetsat consortium. This code corresponds to research studies published in IEEE transaction on Geo-Science and Remote Sensing. It can be freely downloaded on the FLUID web site http://fluid.irisa.fr.

5.3. 3DLayeredMotion software - Estimation of 3D interconnected layered atmospheric motion fields

Participants: Patrick Héas, Etienne Mémin.

This software extends the previous 2D version. It allows (for the first time to our knowledge) the recovery of 3D wind fields from satellite image sequences. As with the previous techniques, the atmosphere is decomposed into a stack of pressure layers. The estimation relies also on pressure data and classification clouds maps and top of clouds pressure maps. In order to recover the 3D missing velocity information, physical knowledge on 3D mass exchanges between layers has been introduced in the data model. The corresponding data model appears to be a generalization of the previous data model constructed from a vertical integration of the continuity equation. This research study has been recently accepted for publication in IEEE trans. on Geo-Science and Remote Sensing. A detailed description of the technique can be found in an Inria research report. The binary of this code can be freely downloaded on the FLUID web site http://fluid.irisa.fr.

5.4. Low-Order-Motion - Estimation of low order representation of fluid motion

Participants: Anne Cuzol, Nicolas Gengembre, Etienne Mémin.

This code enables the estimation of a low order representation of a fluid motion field from two consecutive images. The fluid motion representation is obtained using a discretization of the vorticity and divergence maps through regularized Dirac measure. The irrotational and solenoidal components of the motion fields are expressed as linear combinations of basis functions obtained through the Biot-Savart law. The coefficient values and the basis function parameters are obtained as the minimizer of a functional relying on an intensity variation model obtained from an integrated version of the mass conservation principle of fluid mechanics. Different versions of this estimation are available. The code which includes a Matlab user interface can be downloaded on the FLUID web site http://fluid.irisa.fr. This program corresponds to a research study that has been published in the International Journal on computer Vision.

6. New Results

6.1. Fluid motion estimation

6.1.1. Schlieren image velocimetry

Participants: Patrick Héas, Étienne Mémin.

[In collaboration with G. Artana and P. Minini (Univ. Bueno Aires)]

We have addressed the problem of estimating the motion of fluid flows visualized with the Schlieren technique. Such an experimental visualization system, well known in fluid mechanics, enables the visualization of unseeded flows. It thus allows the capture of phenomena which are impossible to visualize with particle seeding such as natural convection, phonation flow, breath flow, as well as the visualization of large scale structures. Since the resulting images exhibit very low intensity contrasts, classical motion estimation methods based on the brightness constancy assumption (correlation-based approaches, optical flow methods) are inefficient. In order to extract motion fields from these specific images, we have introduced a new energy function composed of i) a specific data model accounting for the fact that the observed luminance is related to the gradient of the fluid density, and ii) a specific constrained div-curl regularization term. The minimization of this energy provides what we believe to be the only existing motion estimator that works properly on Schlieren images.

6.1.2. Multiscale PIV method based on turbulent kinetic energy decay

Participants: Patrick Héas, Dominique Heitz, Etienne Mémin.

We have proposed a new multiscale PIV method based on turbulent kinetic energy decay. The technique is based on scaling power laws describing the statistical structure of turbulence. A spatial regularization constraints the solution to behave through scales as a self similar process via second-order structure function and a given power law. The real parameters of the power-law, corresponding to the distribution of the turbulent kinetic energy decay, have been estimated from a simple hot-wire measurement. The method has been assessed in a turbulent wake flow and grid turbulence through comparisons with HWA measurements and other PIV approaches. Results have indicated that the present method is superior because it accounts for the whole dynamic range involved in the flows.

6.1.3. Dynamic consistent correlation-variational motion estimation

Participants: Johan Carlier, Patrick Héas, Dominique Heitz, Étienne Mémin.

We have proposed a novel collaborative motion estimation scheme dedicated to the measurement of velocity in fluid experimental flows through image sequences. The proposed technique satisfies the Navier-Stokes equations and combines the robustness of correlation techniques with the high density of global variational methods. It can be considered either as a reenforcement of fluid dedicated optical flow methods towards robustness, or as an enhancement of correlation approaches towards dense information. This results in a physics-based technique that is robust with respect to noise and outliers, while providing a dense motion field. The method has been applied on synthetic images and on real experiments in turbulent flows carried out to allow a thorough comparison with a state of the art variational and correlation methods. This work has been recently accepted for publication in the journal Experiments in Fluids.

6.1.4. 3D flows reconstruction from image data

Participants: Dominique Heitz, Étienne Mémin, Sébastien Pellan.

In the continuity of the PhD of Nicolas Papadakis, we want to study techniques for the complete reconstruction of 3D flows from image data sequences. In a first approach we will study the extension to 3D of our different 2D fluid motion estimators from 3D volumetric data obtained through tomographic reconstruction. In a second time, we wish to explore the reconstruction of flows observed simultaneously on several 2D plans. The inclusion of a flow dynamical model will allow us to filter erroneous data and also to reconstruct the missing unobserved components. For computational reasons only large scale models or reduced model are conceivable. We will focus both on experimental flows and on atmospheric flows. In this later case, we will explore techniques for the reconstruction of atmospheric layers observed from satellite images. This will be a continuation of the works conducted on the estimation of layered 2D/3D atmospheric winds.

6.1.5. Stochastic uncertainty models for motion estimation

Participants: Thomas Corpetti, Étienne Mémin.

We have worked on a stochastic interpretation of the motion estimation problem. The usual optical flow constraint equation (that assumes that the points keeps their brightness along time), embedded for instance within a Lucas-Kanade estimator, can indeed be seen as the minimization of a stochastic process under some strong constraints (the luminance as a function of a stochastic process is a martingal with isotropic diffusion). This constraint can be relaxed by imposing weaker assumption on the luminance function and also in introducing anisotropic intensity-based uncertainty assumptions. The amplitude of these uncertainties are jointly computed with the unknown velocity at each point of the image grid. Different estimators have been designed depending on the various hypothesis assumed for the luminance function. The substitution of our new observation terms on a simple Lucas-Kanade estimator improves significantly the quality of the results (on the basis of optical flow datasets with ground truth available on the web) and leads to a local motion estimator without any parameters. We believe that the definition of a dense estimator based on the very same ideas will be very competitive.

6.1.6. Motion estimation techniques for turbulent fluid flows

Participants: Patrick Héas, Dominique Heitz, Étienne Mémin.

[In collaboration with P. Minini (Univ. Bueno Aires)]

Based on scaling laws describing the statistical structure of turbulent motion across scales, we propose a multiscale and non-parametric regularizer for optic-flow estimation. Regularization is achieved by constraining motion increments to behave through scales as the most likely self-similar process given some image data. In a first level of inference, the hard-constrained minimization problem is optimally solved by taking advantage of lagrangian duality. It results in a collection of first-order regularizers acting at different scales. The optimal regularization hyper-parameters at the different scales are obtained by solving the dual problem while in a second inference level, the data-model error variance is obtained using a marginalized maximum likelihood estimation framework. In a third level of inference, the most likely self-similar model given the data is optimally selected by maximization of Bayesian evidence. The motion estimator accuracy is first evaluated on a synthetic image sequence of simulated bi-dimensional turbulence and then on a real meteorological image sequence. Results obtained with the proposed physical based approach exceed the best state of the art results. This work has been published in several conference including the "International Conference on Computer Vision" (ICCV) 2009, "Turbulent Mixing and Beyond" (TMB) 2009 and the "International Conference on Geosciences and Remote Sensing" (IGARSS) 2009.

6.1.7. Wavelet basis for multi-scale motion estimation

Participants: Pierre Dérian, Patrick Héas, Étienne Mémin.

In this work we have devised proper scale-space representations for multi-scale analysis of turbulent flows from images. Decomposing motion on a wavelets basis provides an efficient framework to estimate motion from images, while constraining the solution to possess a given regularity. In this perspective, we have defined a family of optic-flow spatial regularizer of various orders by simply varying the vanishing moments of the wavelets used for decomposition. Moreover, fractal behaviors of the motion field increments have also been introduced as prior models for regularization. Indeed, decomposing motion on a wavelet basis provides an efficient way to constrain the solution to be self-similar. This is achieved by modeling the decay of the wavelet coefficients through scales. The proposed methods are currently under development.

6.1.8. Bayesian inference of hyper-parameters and models in motion estimation

Participants: Patrick Héas, Étienne Mémin.

Bayes' rule provides a nice framework for motion estimation from image sequences. To enable Bayesian modeling, in this work we first describe the optic-flow estimation problem from a probabilistic perspective. This well-known problem relies on a hierarchical model linking the image intensity function variable, the motion field variable, hyper-parameters composed of the likelihood and prior model inverse variances and of robust parameters, and finally the observation and prior model. The variable dependence can thus be expressed as a 4-level hierarchy. Applying Bayes' rule on this hierarchy, we obtain three levels of inference, which enables us to obtain, by marginalization out intermediate variables, a direct dependence of the variable of interest to the image intensity function. Thus, estimates of regularization parameters, of robust parameters associated to semi-quadratic norms of M-estimators, and of observation and prior models are inferred in a maximum likelihood sense while maximizing jointly the motion field a posteriori probability. The quality of the method is demonstrated on synthetic and real two-dimensional turbulent flows and on several computer vision scenes of the "Middlebury" data-base.

6.2. Tracking and data assimilation

6.2.1. Stochastic filtering for fluid motion tracking Participants: Sébastien Béyou, Étienne Mémin.

We investigated the study of a recursive Bayesian filter for tracking velocity fields of fluid flows. The filter combines an Ito diffusion process associated to 2d vorticity-velocity formulation of Navier-Stokes equation and discrete image error reconstruction measurements. In contrast to usual filters designed for visual tracking problems, our filter combines a continuous law for the description of the vorticity evolution with discrete image measurements. We resort to a Monte-Carlo approximation based on particle filtering. The designed tracker provides a robust and consistent estimation of instantaneous motion fields along the whole image sequence. In order to handle a state space of reasonable dimension for the stochastic filtering problem, the motion field is represented as a combination of adapted basis functions. The basis functions are derived from a mollification of Bio-Savart integral and a discretization of the vorticity and divergence maps of the fluid vector field. The output of such a tracking is a set of motion fields along the whole time range of the image sequence. As the time discretization is much finer than the frame rate, the method provides consistent motion interpolation between consecutive frames. In order to reduce further the dimensionality of the associated state space when we are facing a large number of motion basis functions, we have explored a new dimensional reduction approach based on dynamical systems theory. The study of the stable and unstable directions of the continuous dynamics enables to construct an adaptive dimension reduction procedure. It consists in sampling only in the unstable directions, while the stable ones are treated deterministically. This work has been recently accepted for publication in IEEE Journal on Pattern Analysis and Machine Intelligence.

When the likelihood of the measurement can be modeled as Gaussian law, we have also investigated the use of so-called ensemble Kalman filtering for fluid tracking problems. This kind of filters introduced for the analysis of geophysical fluids is based on the Kalman filter update equation. Nevertheless, unlike traditional Kalman filtering setting, the covariances of the estimation errors, required to compute the so called Kalman gain, relies on an ensemble of forecasts. Such a process gives rise to a Monte Carlo approximation for a family of non-linear stochastic filters enabling to handle state spaces of large dimension. We have recently proposed an extension of this technique that combines sequential importance sampling and the propagation law of ensemble Kalman filter. This technique leads to an ensemble Kalman filter with an improve efficiency. This strategy appears to be a generalization of the so called optimal importance sampling proposed within the PhD of Elise Arnaud in the context of partial conditional Gaussian trackers. The bridge of this setup with ensemble Kalman filters is described in the PhD manuscript of Nicolas Papadakis.

The tracking experiments have been conducted on fluid experimental image sequences provided by the CEMAGREF and ONERA and also on satellite meteorological sequences supplied by the LMD (Laboratoire de Météorologie Dynamique) and the EUMETSAT consortium.

6.2.2. Variational Data Assimilation for Convective Cells Tracking

Participants: Thomas Corpetti, Étienne Mémin.

This work focuses on the tracking and analysis of convective clouds systems from Meteosat Second Generation images. The highly deformable nature of convective clouds, the complexity of the physic processes involved, but also the partially hidden measurements available from image data make difficult a direct use of conventional image analysis techniques for tasks of detection, tracking and characterization. We face these issues using variational data assimilation tools. Such techniques enable to perform the estimation of an unknown state function according to a given dynamical model and to noisy and incomplete measurements. The system state we are setting in this study for the system clouds representation is composed of two nested curves corresponding to the exterior frontiers of the clouds and to the interior coldest parts (heart) of the convective clouds. Since no reliable simple dynamical model exists for such phenomena at the image grid scale, the dynamics on which we are relying has been directly defined from image based motion measurements and takes into account an uncertainty modeling of the curves dynamics along time. In addition to this assimilation technique, we also investigate how each cell of the recovered clouds system can be labeled and associated to characteristic parameters (birth or death time, mean temperature, velocity, growth, etc.) of great interest for meteorlogists.

6.2.3. Atmospheric motion estimation with pressure image assimilation

Participants: Thomas Corpetti, Héas Patrick, Étienne Mémin.

The complexity of the laws of dynamics governing 3D atmospheric flows associated with incomplete and noisy observations make the recovery of atmospheric dynamics from satellite image sequences very difficult. We addressed the challenging problem of estimating physical sound and time-consistent horizontal motion fields at various atmospheric depths for a whole image sequence. Based on a vertical decomposition of the atmosphere, we proposed a dynamically consistent atmospheric motion estimator relying on a multi-layer dynamic model. This estimator is based on an optimal control scheme with uncertainty terms (weak constraint variational data assimilation) and is applied on noisy and incomplete pressure difference observations derived from satellite images. The dynamic model is a simplified vorticity-divergence form of a multi-layer shallow-water model. Average horizontal motion fields are estimated for each layer. The performance of the proposed technique has been assessed using synthetic examples and using real world meteorological satellite image sequences. In particular, it is shown that the estimator enables exploiting the finest spatio-temporal image structures and succeeds in characterizing motion at small spatial scales of the image grid. This work has been recently published in the journal Tellus Series A: Dynamic Meteorology and Oceanography.

6.2.4. Reduced order models for wake flows

Participants: Johan Carlier, Étienne Mémin, Véronique Souchaud.

In this work we have studied techniques allowing a robust estimation of reduced order model (ROM) for wake flows from flow velocity field experimental data. The proposed method relies on a proper orthogonal decomposition method (POD) and a Galerkin projection. The POD technique allows the extraction of a reduced number of functions or modes that describes at best the flow's velocity field (in the sense of a mean kinetic energy reconstruction error). Galerkin projection of Navier Stokes equation onto these modes supplies a system of ordinary non linear equations. The sole dimension reduction from Galerkin procedure does not assure the convergence and stability of solutions. Recently an efficient POD data assimilation scheme we previously proposed allowed us to handle this instability problem in the time range of the data sequence. In order however to provide an unconditionally stable system and to be able to provide a stable flow prediction beyond the data sequence time range, recent studies on hydrodynamic stability in wake flows suggest model modifications of the POD-Galerkin ROM in agreements with center manifold theory. In this context we have proposed to couple a data assimilation strategy with center manifold theory to achieve improvements for the POD-based ROM from velocity fields experimental data. For the moment the method has been validated only on noise free synthetic data provided by direct numerical simulations (DNS).

6.2.5. Optimal control techniques for the coupling of large eddy dynamical systems and image data

Participants: Alejandro Gronskis, Dominique Heitz, Etienne Mémin.

Real flows have an extent of complexity that prevents any set of sensors or any state of the art numerical simulation from providing enough information to describe them completely. Even with the highest available capacities in term of sensors sensitivity, space-time coverage, grid refinement, and computational power there will always remain at least a lack of resolution and some missing input about the actual boundary conditions. That is obviously true for the complex flows encountered in industrial and natural conditions, but remains also an obstacle even for standard academic flows thoroughly investigated in research conditions. This unavoidable deficiency of the experimental techniques can be greatly improved by their coupling with dynamical models and numerical simulations. The parallel advances in sensors, acquisition, and treatment and computer efficiency allow the mixing of experimental and simulated data produced at compatible scales in space and time. The inclusion of dynamical models as constraints of the data analysis process brings a guarantee of coherency based on fundamental equations known to correctly represent the dynamics of the flow (e.g. Navier Stokes equations). Conversely, the injection of experimental data into simulations ensures some fitting of the model with reality. When used with the correct level of expertise to calibrate the models at the relevant scales, regarding data validity and the targeted representation scale, this collaboration represents a powerful tool for the analysis and reconstruction of the flows. Automated back and forth sequencing between data integration and calculations have to be elaborated for the different types of flows with a correct adjustment of the observed and modeled scales. This appears more and more feasible when considering the sensitivity, the space resolution and above all the time resolution that the imaging sensors are reaching now. Optimal control theory and variational data assimilation technique offers a now well-established framework to operate such a coupling between data and a dynamical model.

In this work we aim at investigating the use of optimal control techniques for the coupling of Large Eddies Simulation (LES) techniques and 2D image data. The aim is to reconstruct a 3D flow from a set of simultaneous time resolved 2D image sequences visualizing the flow on a set of 2D plans enlightened with laser sheets. This approach will be experimented on shear layer flows and on wake flows generated on the wind tunnel of the Cemagref Rennes. Within this study we whish also to explore techniques that will allow enriching large-scale dynamical models by the introduction of uncertainty terms or through the definition of subgrid models from the image data. This research theme is related to the issue of turbulence characterization from image sequences. Instead of predefined turbulence models, we aim here at tuning from the data the value of coefficients involved in traditional LES subgrid models or in longer-term goal to learn empirical subgrid models directly from image data. An accurate modeling of this term is essential for Large Eddies Simulation as it models all the non resolved motion scales and their interactions with the large scales.

6.2.6. Stochastic filtering technique for the tracking of closed curves

Participants: Christophe Avenel, Etienne Mémin, Patrick Pérez.

We have proposed a filtering methodology for the visual tracking of closed curves. Opposite to works of the literature related to this issue, we consider here a curve dynamical model based on a continuous time evolution law with different noise models. This led us to define three different stochastic differential equations that capture the uncertainty relative to curve motions. This new approach provides a natural understanding of classical level-set dynamics in terms of such uncertainties. These evolution laws have been combined with various color and motion measurements to define probabilistic state space models whose associated Bayesian filters can be handled with particle filters. This on going work will be continued within extensive curve tracking experiments and extended to the tracking of other very high dimensional entities such as vector fields and surfaces.

6.3. Analysis and modeling of turbulent flows

6.3.1. Experimental study of turbulent planar jet issuing in an uniform co-flow

Participants: Johan Carlier, Jean Youssef.

A wind tunnel was especially designed to study the development of a jet issuing in an uniform co-flow. This flow has been explored with classical Hot- Wire Anemometry (Constant Temperature Anemometry) and Particle Image Velocimetry systems. It has been observed that the co-flow modifies the similarity behaviour of the planar jet which behaves either as a strong jet or as a wake flow. The influence of the Reynolds number and shear parameter on the similarity behaviour of the stress tensor has been analyzed. Based on these results, the coupling of the velocity and temperature dynamics will be studied in non-isothermal configurations using a new variable temperature hot-wire anemometry method (Parametrizable CTA) especially designed for the simultaneous measurement of velocity and temperature at the same point.

6.3.2. Mixing layers between a uniform flow and a shear flow

Participants: Toutou Ndiaye, Dominique Heitz.

We have addressed the analysis and modelling of non canonical turbulent mixing layers between a uniform flow and a shear flow. From a parametric study by bidimensional direct numerical simulations two mixing layer configurations between a uniform flow and a shear flow have been selected. These two configurations share the same shear flow but have a different uniform flow. The shear flow was obtained with curved gauze. However the theoretical shear parameter predicted by the literature is different from the value obtained by experiments. In order to study these discrepancies, the flow through a gauze was studied by particle image velocimetry. This allowed the general modeling of the uniform flow through curved wire gauze, leading to linear mean velocity profiles. From a hot-wire anemometry study of the two flow configurations it was observed that one flow behaves like a mixing layer whereas the other flow yields a wake behaviour. The mixing layer indicates an increasing turbulent kinetic energy along its longitudinal development, while the wake exhibits an asymmetry.

6.3.3. Experimental study of turbulence in an non-isothermal mixing layer

Participants: Kodjovi Sodjavi, Johan Carlier.

A wind tunnel was designed to study the behaviour of the turbulence in a non- isothermal mixing layer. This flow is measured with classical Hot-Wire Anemometry (Constant Temperature Anemometry) and Particle Image Velocimetry systems. It was also explored with a new variable temperature hot-wire anemometry method (Parametrizable CTA) especially designed for the simultaneous measurement of velocity and temperature at the same point. We focus our attention on the influence of the control parameters (Reynolds number, shear parameter and Richardson number) on the flow statistics and the validity of Kolmogorov and Yaglom equation based on structure functions which can be evaluated with the new PCTA method.

6.3.4. Experimental studies for the assessment of turbulence statistical models

Participants: Patrick Héas, Dominique Heitz, Etienne Mémin.

[In collaboration with G. Artana and P. Minini (Univ. Bueno Aires)]

Selecting directly from images the most likely scaling motion priors enables the recovery of physical quantities related to the energy flux and the flow regularity. Such measurements are of major interest for turbulence studies. In particular, determining the energy flux across scales and characterizing intermittency is very important to assess the relevance of the statistical models proposed for atmospheric turbulence. Although, the measurement of flux and atmospheric flow regularity has already been obtained previously using in situ data, it required an important measurement campaign lasting several years based on sensors placed on airplanes. Therefore, the proposed motion estimation technique described above represents an attractive tool since it enables the direct estimation of these quantities from a couple of images. A paper concerning an atmospheric turbulence study using Meteosat Second Generation (MSG) images is currently under revision for publication in the "Journal of Fluid Mechanics" (JFM). Experimental studies of three-dimensional turbulence behind a grid or in the wake of a cylinder have also been published in the conference on Particle Imagery and Velocimetry (PIV) 2009. New experiments for the assessment of turbulence statistical models are currently going on in collaboration with the laboratory of fluid mechanics and turbulence scientists in Argentina. They focus on two-dimensional turbulence of soap films visualized with a Schlieren imagery system. The goal of this work is to validate experimentally the theoretical model predicting non-intermittent inverse energy cascades in pure two-dimensional flows

6.4. Visual servoing approach for fluid flow control

6.4.1. Visual servoing for 2D plane Poiseuille flow

Participants: Christophe Collewet, Roméo Tatsambon.

We focus here on the particular case of the 2D plane Poiseuille flow, i.e. a flow between two infinite parallel planes. The most usual way to control this flow is to use boundary transpiration. In that case, suction and blowing of fluid with zero net mass flow are performed along a wall. Our goal is to control this flow to stabilize it at a high Reynolds number ($\approx 10^4$). Indeed, it is well known that this flow is unstable for a such Reynolds number value. Despite the fact that it is one of the simplest and best understood flows in fluid mechanics, its control is still an open issue. This kind of controlled flow has become a standard benchmark problem for the validation of various control scheme approaches. Usually, the streamwise shear stress component at a point belonging to the wall is used as the output of the system in order to control scheme. Of course, as mentioned in section 3.4, the main challenge is to obtain the interaction matrix related to such features. More precisely, our goal is to obtain an analytic form of this matrix in order to design an efficient control law and to derive convergence properties.

6.4.2. Brightness consistancy models for visual servoing

Participants: Christophe Collewet, Thomas Corpetti.

Most of computer vision-based applications rely on low level algorithms such as matching, features tracking, or optical flow computations for example. Such approaches are based on a relation that links the luminance of a physical point at time t to its luminance at a later time t + dt due to a relative motion of the observer with respect to that scene or to other events like illumination changes. Nevertheless, due to the complexity of this relation, most often, the algorithms aforementioned are based on the temporal luminance constancy hypothesis leading to well known *optical flow constraint equation* [28]. However, it is well known that this constraint can be easily violated. In our previous paper [21], we have revisited this constraint and provided a new optical flow constraint. It has been validated in the context of 3D target tracking by visual servoing. Our goal is to validate it the context of optical flow where more complex motion and illumination changes occur.

7. Contracts and Grants with Industry

7.1. MSR-Inria Video data mining for environmental and social sciences

Participants: Sai Gorthi, Etienne Mémin, Patrick Pérez.

duration 36 months.

This contract takes place in the context of the joint Microsoft-Inria research laboratory. It involves two other Inria project-teams, Willow and Lear. The projects is composed of three fairly disjoint sub-projects. Fluminance contributes to two of them: (i) Mining dynamical remote data with applications in computational ecology and environmental science; (ii) Mining TV broadcasts with applications to sociology. In the first sub-project, we aim at combining various low and mid-level video analysis tools (shot detection, camera motion characterization, visual tracking, object recognition, human action recognition) for the analysis and annotation of human actions and interactions in video segments to assist -and provide data for- studies of consumer trends in commercials, political event coverage in newscasts, and class- and gender-related behavior patterns in situation comedies, for example. In the second one, we aim at designing new tools for the detection of salient changes in multi-temporal satellite images (with application to assessment of natural damages, consequences of climate modifications, and changes caused by human action in urban or natural environments), and, in the longer term, for the detection, identification and tracking of dynamics meteorological events, with application to risk assessment and weather forecast.

8. Other Grants and Activities

8.1. National initiatives

8.1.1. ANR STANDS-MSG

Participants: Thomas Corpetti, Etienne Mémin.

duration 36 months.

This ANR project entitled "Spatio-temporal Analysis of deformable structures in Meteosat Second Generation images" aims at developing methods for the analysis of deformable structures in meteorological images. More precisely, within this project we will focus on two meteorological phenomenon: the convective cells and sea breeze circulation. The first type of cloud system is responsible of dangerous meteorological events such as strong showers. Their monitoring is thus very important. See breezes influence deeply the climate of coastal regions. The comprehension of the daily and seasonal evolution of see breeze fronts is of great importance for local weather forecasting. The goal of this project will be to propose tools based on appropriate physical evolution laws for the tracking and analysis of these events. This project involves computer vision scientists from different groups, climatologists and meteorologists.

8.1.2. STIC-AMSUD Modeling voice production

Participant: Etienne Mémin.

duration 36 months.

This project aims at studying both, theoretically and experimentally, the phenomena involved in vocal fold oscillations, towards the elaboration of performing vocal production models, for application in voice and speech technology. It gathers partners from Brazil (PUCRS, UFF), Argentina (UBA) and France (LIMSI,ICP, IRISA).

8.1.3. CNRS-INRIA MINCyT: Reduced dynamical modeling

Participants: Johan Carlier, Etienne Mémin.

duration 36 months.

This bilateral collaboration project between Argentina and France is a three years project that gathers the ESPCI (J.E. Weisfreid) the ENS-LMD (M. Farge) and the University of Buenos Aires (G. Artana). It concerns the study of estimation techniques of low order dynamical from image sequences with the aim of providing recursive and adaptable techniques to go toward the possibility of flow control through visual servoing.

8.1.4. ANR-COSINUS PREVASSEMBLE: Ensemble methods for assimilation of observaions and for prevision in Meteorology and Oceanography

Participants: Sébastien Béyou, Etienne Mémin.

duration 36 months.

The purpose of this project is to further study ensemble methods -, and to develop their use for both assimilation of observations and prediction. Among the specific questions to be studied are the theory of Particle Filters ane Ensemble Kalman Filters, the possibility of taking temporal correlation into account in ensemble assimilation, the precise assessment of what can and cannot be achieved in ensemble prediction, and the objective validation of ensemble methods.

The partners of this project are Laboratoire de Météorologie Dynamique/ENS (leader), Météo-France and three INRIA groups (ALEA, ASPI, FLUMINANCE).

8.1.5. ANR SYSCOMM MSDAG: MultiScale Data Assimilation in Geophysics

Participants: Johan Carlier, Pierre Dérian, Patrick Héas, Dominique Heitz, Etienne Mémin.

duration 36 months.

Changing scale is a well-known topic in physics (geophysics, fluid mechanics and turbulence, theoretical and statistical physics, mechanics, porous media, etc.) It has lead to the creation of powerful sophisticated mathematical tools: renormalization, homogenization, etc. These ideas are also used in numerical analysis (the so-called multigrid approach) for solving efficiently partial differential equations. Data assimilation in geophysics is a set of methods that allows to combine optimally numerical models in large spaces with large dataset of observations. At the confluence of these two topics, the goal of this project is to study how to embed the change of scales (a multiscale point of view) issue into the framework of geophysical data assimilation, which is a largely unexplored subject.

The partners of this 3 years project are the CEREA/ CLIME INRIA group (leader), the LSCE/CEA, the INRIA groups MOISE and FLUMINANCE.

8.1.6. ANR SYSCOMM GeoFluids:

Participants: Johan Carlier, Alejandro Gronskis, Patrick Héas, Dominique Heitz, Etienne Mémin, Véronique Souchaud.

duration 48 months.

The project Geo-FLUIDS focuses on the specification of tools to analyse geophysical fluid flows from image sequences. Geo-FLUIDS aims at providing image-based methods using physically consistent models to extract meaningful features describing the observed flow and to unveil the dynamical properties of this flow. The main targeted application domains concern Oceanography and Meteorology . The project consortium gathers the INRIA research groups: FLUMINANCE (leader), CLIME, IPSO, and MOISE. The group of the "Laboratoire de Météorologie Dynamique" located at the ENS Paris, the IFREMER-CERSAT group located at Brest and the METEOFRANCE GMAP group in Toulouse.

8.1.7. Other involvements

- The Fluminance is involved in the French network GDR "Structure de la Turbulence et Mélange".
- The Flumiance group participates to the French network GDR "Contrôle Des Décollements".

8.2. Bilateral international co-operation

8.2.1. Collaboration with University of Buenos-Aires, Inria associate team FIM

Participants: Guillermo Artana, Bruno Cernuschi-Frias, Tomas Crivelli, Patrick Bouthemy, Étienne Mémin, Jian-Feng Yao, Patrick Héas.

The Inria associate team FIM ("Fluidos e Imágenes de Moviemento") is concerned with the analysis of fluid flow from image sequences. It was created in December 2004. This long-term and intensive cooperation involves two groups from the Engineering Faculty of the University of Buenos-Aires: the Signal processing group headed by Professor Bruno Cernuschi-Friàs and the Fluid Mechanics group headed by Professor Guillermo Artana. Two main themes are investigated. The first one deals with experimental visualization and embeds modeling, motion measurement and analysis of fluid flows. The second one is concerned with the modeling, segmentation and recognition of dynamic textures in videos of natural fluid scenes (sea-waves, rivers, smoke, moving foliage, etc...).

9. Dissemination

9.1. Leadership within scientific community

- + Editorial boards of journals
 - E. Mémin is Associate Editor for the Image and Vision Computing Journal.
- + Conference organization
 - D. Heitz organized a workshop of the GdR CNRS Structure of Turbulence entitled "Coupling data and models" held in Rennes, January 2008.
- + *Technical program committees of conferences*
 - C. Collewet: TPC member of ORASIS'09.
 - E. Mémin: TPC member of ICCV'09.
- + Ph.D. reviewing
 - E. Mémin: M. Druon (SIC Université de Poitiers), D. Van Tran (LABSTICC U. de Bretagne Sud)
 - D. Heitz: T.D. Nguyen (INSA Rennes).
- + Project reviewing, consultancy, administrative responsibilities
 - C. Collewet is member of the cemagref evaluation committee

9.2. Teaching

- Master STI "Signal, Telecommunications, Images", University of Rennes 1, (E. Mémin : statistical image analysis).
- DIIC INC, Ifsic, University of Rennes 1 (E. Mémin : Motion analysis)
- INSA Rennes, 2nd year (J. Youssef: Introduction to Fluid Mechanics)

9.3. Participation in seminars, invitations, awards

- C. Collewet was chair of the session "Active-Contour and Level-Set Based Segmentation" at ICIP'09
- P. Héas gave an invited talk at the conference "Turbulent Mixing and Beyond".
- E. Mémin has been invited to give talks on Fluid flows analysis from image sequence at the CNRM Météo-France; he gaves an invited talk at the STAR workshop on visual tracking of entities with non-linear dynamics; he gaves an invited talk to a colloquium organized in the honor of F.-X Le Dimet;

10. Bibliography

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National Peer-Reviewed Conference/Proceedings

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